

## REFERENCES

- [1] Bates, E. T., & Wiest, L. R. (2004). Impact of Personalization of Mathematical Word Problems on Student Performance. *Mathematics Educator*, 14(2), 17-26.
- [2] Cummins, D. D., Kintsch, W., Reusser, K., & Weimer, R. (1988). The role of understanding in solving word problems. *Cognitive psychology*, 20(4), 405-438.
- [3] (2013, May 20). Retrieved February 24, 2017, from [http://www.moe.gov.lk/english/images/publications/Annual\\_performance\\_Report2013/Annual\\_performance\\_report\\_e.pdf](http://www.moe.gov.lk/english/images/publications/Annual_performance_Report2013/Annual_performance_report_e.pdf), Annual Performance Report.
- [4] Bennett, R. E. (2011). Automated scoring of constructed-response literacy and mathematics items. White paper, Educational Testing Service.
- [5] Lan, A. S., Vats, D., Waters, A. E., & Baraniuk, R. G. (2015, March). Mathematical language processing: Automatic grading and feedback for open response mathematical questions. In Proceedings of the Second (2015) ACM Conference on Learning@ Scale (pp. 167-176). ACM.
- [6] Badger, M. (2013). Problem-solving in undergraduate mathematics and computer aided assessment (Doctoral dissertation, University of Birmingham).
- [7] (2010, April 04). Retrieved February 24, 2017, from <http://www.open.ac.uk/openmarkexamples/numeric-response>, Numerical Response.
- [8] Fife, J. H. (2011). Automated scoring of CBAL mathematics tasks with m-rater. Research Memorandum, ETS RM-11-12.
- [9] Fife, j. H. (2013). Automated scoring of Mathematics tasks in the common core era: enhancements to m-rater in support of CBAL Mathematics and the common core assessments. ETS research report series, 2013(2).
- [10] Hilton III, J. L., Gaudet, D., Clark, P., Robinson, J., & Wiley, D. (2013). The adoption of open educational resources by one community college math department. *The International Review of Research in Open and Distributed Learning*, 14(4).
- [11] Campbell, J. I. (1994). Architectures for numerical cognition. *Cognition*, 53(1), 1-44.
- [12] Luneta, K., & Makonye, P. J. (2010). Learner Errors and Misconceptions in Elementary Analysis: A Case Study of a Grade 12 Class in South Africa. *Acta Didactica Napocensia*, 3(3), 35-46.

- [13] Veloo, A., Krishnasamy, H. N., & Abdullah, W. S. W. (2015). Types of Student Errors in Mathematical Symbols, Graphs and Problem-Solving. *Asian Social Science*, 11(15), 324.
- [14] Erabadda B., "Automatic identification of errors in multi-step answers to algebra questions" in Proceedings of the 17th IEEE International Conference on Advanced Learning Technologies (ICALT), 2017.(Accepted)
- [15] Landauer, T. K., Foltz, P. W., & Laham, D. (1998). An introduction to latent semantic analysis. *Discourse processes*, 25(2-3), 259-284.
- [16] Li, Y., McLean, D., Bandar, Z. A., O'shea, J. D., & Crockett, K. (2006). Sentence similarity based on semantic nets and corpus statistics. *IEEE transactions on knowledge and data engineering*, 18(8), 1138-1150.
- [17] Zhao, J., Zhu, T. T., & Lan, M. (2014). Ecnu: One stone two birds: Ensemble of heterogenous measures for semantic relatedness and textual entailment. *Proceedings of the SemEval*, 271-277.
- [18] Klai, S., Kolokolnikov, T., & Van den Bergh, N. (2000). Using Maple and the web to grade mathematics tests. In *Advanced Learning Technologies, 2000. IWALT 2000. Proceedings. International Workshop on* (pp. 89-92). IEEE.
- [19] Ritter, S., Anderson, J. R., Koedinger, K. R., & Corbett, A. (2007). Cognitive Tutor: Applied research in mathematics education. *Psychonomic bulletin & review*, 14(2), 249-255.
- [20] Melis, E., & Siekmann, J. (2004, June). Activemath: An intelligent tutoring system for mathematics. In *International Conference on Artificial Intelligence and Soft Computing* (pp. 91-101). Springer Berlin Heidelberg.
- [21] Funk, N. (2000). JEP-Java Math Expression Parser. Online document.
- [22] Joyner, D., Čertík, O., Meurer, A., & Granger, B. E. (2012). Open source computer algebra systems: SymPy. *ACM Communications in Computer Algebra*, 45(3/4), 225-234.
- [23] Gomaa, W. H., & Fahmy, A. A. (2012). Short answer grading using string similarity and corpus-based similarity. *International Journal of Advanced Computer Science and Applications (IJACSA)*, 3(11).
- [24] Hale, M. M. (1998). A comparison of WordNet and Roget's taxonomy for measuring semantic similarity. arXiv preprint cmp-lg/9809003.

- [25] Resnik, P. (1995). Using information content to evaluate semantic similarity in a taxonomy. arXiv preprint cmp-lg/9511007.
- [26] Wu, Z., & Palmer, M. (1994, June). Verbs semantics and lexical selection. In Proceedings of the 32nd annual meeting on Association for Computational Linguistics (pp. 133-138). Association for Computational Linguistics.
- [27] Tayal, M. A., Raghuvanshi, M. M., & Malik, L. (2014, December). Word net based Method for Determining Semantic Sentence Similarity through various Word Senses. In Proceedings of the First Joint Conference on Lexical and Computational Semantics.
- [28] Mohler, M., & Mihalcea, R. (2009, March). Text-to-text semantic similarity for automatic short answer grading. In Proceedings of the 12th Conference of the European Chapter of the Association for Computational Linguistics (pp. 567-575). Association for Computational Linguistics.
- [29] Hirst, G., & St-Onge, D. (1998). Lexical chains as representations of context for the detection and correction of malapropisms. WordNet: An electronic lexical database, 305, 305-332.
- [30] Jiang, J. J., & Conrath, D. W. (1997). Semantic similarity based on corpus statistics and lexical taxonomy. arXiv preprint cmp-lg/9709008.
- [31] Leacock, C., & Chodorow, M. (1998). Combining local context and WordNet sense similarity for word sense identification. WordNet, an Electronic Lexical Database.
- [32] Lesk, M. (1986, June). Automatic sense disambiguation using machine readable dictionaries: how to tell a pine cone from an ice cream cone. In Proceedings of the 5th annual international conference on Systems documentation (pp. 24-26). ACM.
- [33] Lin, D. (1998, July). An information-theoretic definition of similarity. In ICML (Vol. 98, No. 1998, pp. 296-304).
- [34] Mohler, M., Bunescu, R., & Mihalcea, R. (2011, June). Learning to grade short answer questions using semantic similarity measures and dependency graph alignments. In Proceedings of the 49th Annual Meeting of the Association for Computational Linguistics: Human Language Technologies-Volume 1 (pp. 752-762). Association for Computational Linguistics.

- [35] Alves, A. O., Ferrugento, A., Lourenço, M., & Rodrigues, F. (2014). Asap: Automatic semantic alignment for phrases. *SemEval 2014*, 104.
- [36] Bestgen, Y. (2014). CECL: a new baseline and a non-compositional approach for the Sick benchmark. *SemEval 2014*, 160.
- [37] Agirre, E., Banea, C., Cardie, C., Cer, D., Diab, M., Gonzalez-Agirre, A., ... & Wiebe, J. (2014, August). Semeval-2014 task 10: Multilingual semantic textual similarity. In Proceedings of the 8th international workshop on semantic evaluation (SemEval 2014) (pp. 81-91). Association for Computational Linguistics Dublin, Ireland.
- [38] Marelli, M., Bentivogli, L., Baroni, M., Bernardi, R., Menini, S., & Zamparelli, R. (2014). Semeval-2014 task 1: Evaluation of compositional distributional semantic models on full sentences through semantic relatedness and textual entailment. SemEval-2014.
- [39] Boehme, R. F., Fairweather, P. G., Farooq, U., Lam, D., & Singley, K. (2008). U.S. Patent Application No. 12/051,347.
- [40] Li, G., Li, L., Su, W., & Zhao, Y. (2006). Design and implementation of MAML. In Proceedings of ATCM.
- [41] Ambekar, D. (2015). Evaluation of essays using incremental training for Maximizing Human-Machine agreement (Doctoral dissertation, Indian Institute of Technology, Bombay).
- [42] Livne, N. L., Livne, O. E., & Wight, C. A. (2007). Can automated scoring surpass hand grading of students' constructed responses and error patterns in mathematics. *MERLOT Journal of Online Learning and Teaching*, 3(3), 295-306.
- [43] Pellegrino, J. W., & Goldman, S. R. (1987). Information processing and elementary mathematics. *Journal of Learning Disabilities*, 20(1), 23-32.
- [44] Norman, D. A. (1981). Categorization of action slips. *Psychological review*, 88(1), 1.
- [45] Feng, M., Heffernan, N., & Koedinger, K. (2010). Student modeling in an intelligent tutoring system. *Intelligent tutoring systems in e-learning environments: Design, implementation and evaluation*, 208-236.
- [46] Arroyo, I., Beal, C., Murray, T., Walles, R., & Woolf, B. P. (2004, August). Web-based intelligent multimedia tutoring for high stakes achievement tests. In

International Conference on Intelligent Tutoring Systems (pp. 468-477). Springer Berlin Heidelberg.

[47] (2014). Retrieved February 24, 2017, from <http://mathspring.org/>, University of Massachusetts

[49] Welgama, V., Herath, D. L., Liyanage, C., Udalamatta, N., Weerasinghe, R., & Jayawardana, T. (2011). Towards a sinhala wordnet. In Proceedings of the Conference on Human Language Technology for Development.

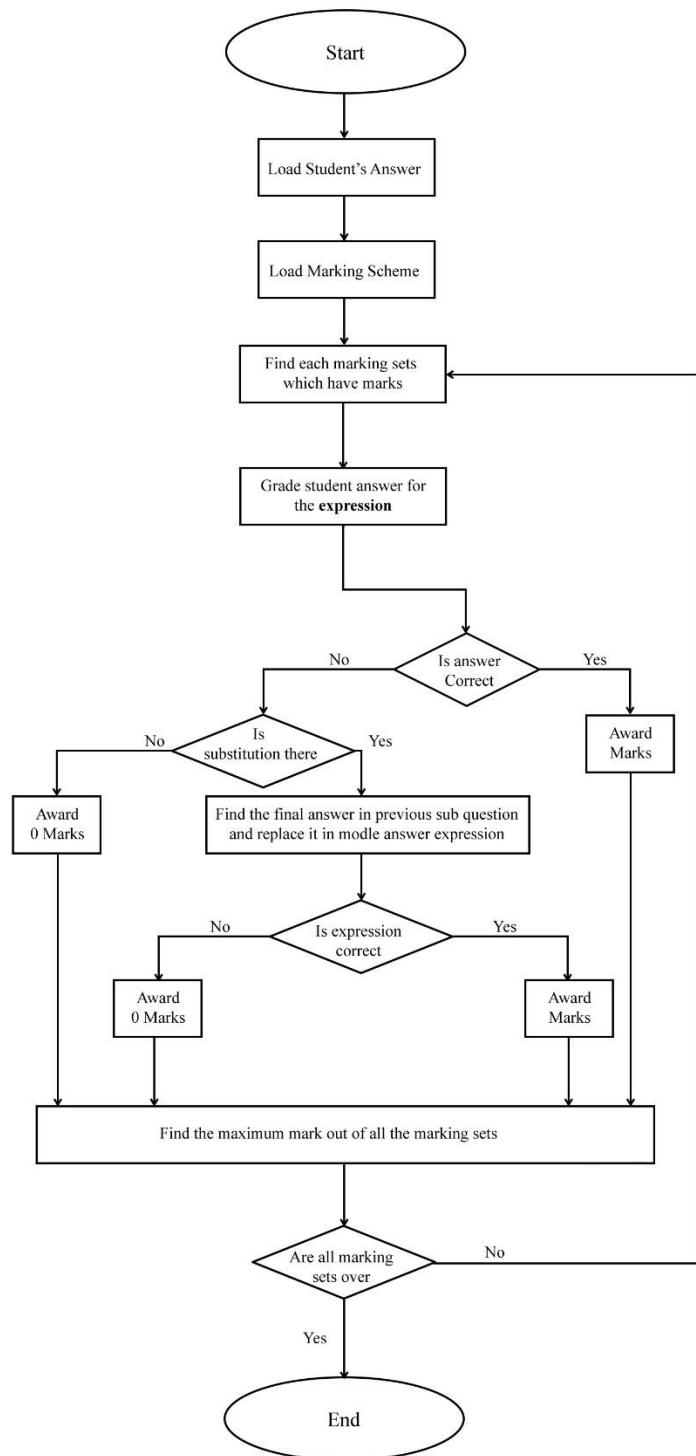
[50] Wijesiri, I., Gallage, M., Gunathilaka, B., Lakjeewa, M., Wimalasuriya, D. C., Dias, G., ... & De Silva, N. (2014). Building a WordNet for Sinhala. Volume editors, 100.

[51] Corley, C., & Mihalcea, R. (2005, June). Measuring the semantic similarity of texts. In Proceedings of the ACL workshop on empirical modeling of semantic equivalence and entailment (pp. 13-18). Association for Computational Linguistics.

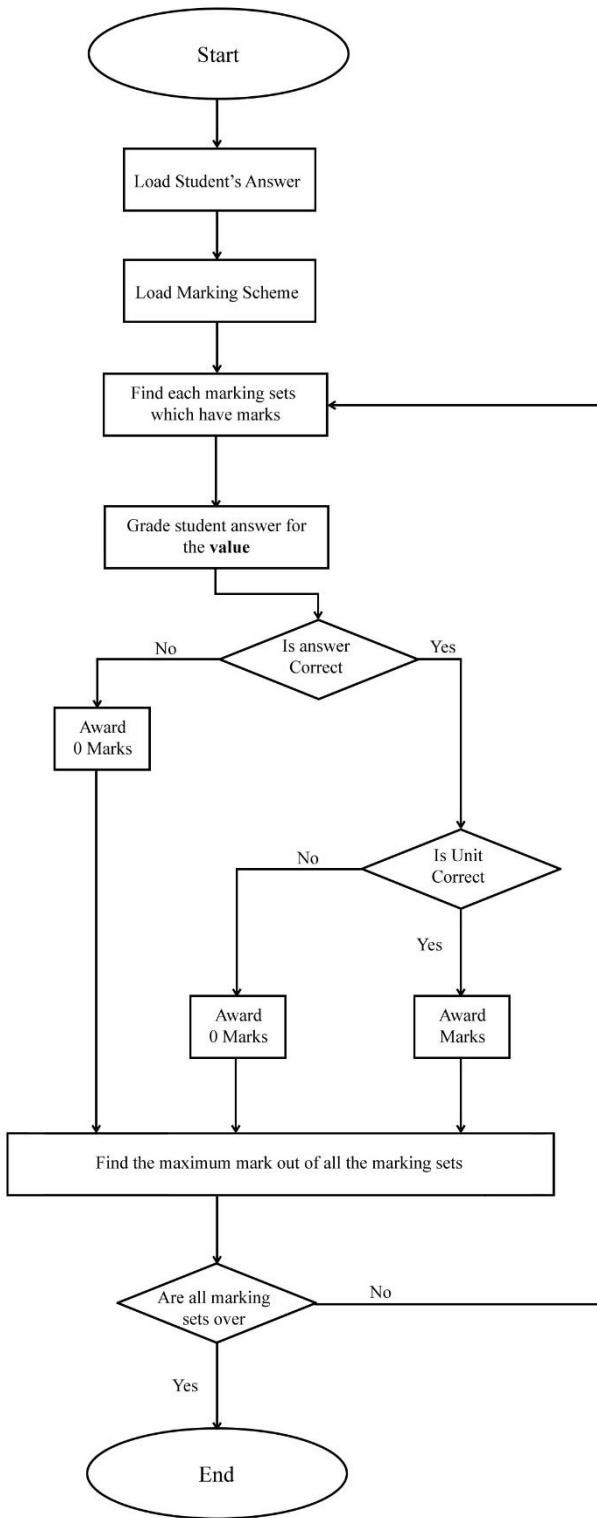
[52] Budanitsky, A., & Hirst, G. (2001, June). Semantic distance in WordNet: An experimental, application-oriented evaluation of five measures. In Workshop on WordNet and other lexical resources (Vol. 2, pp. 2-2).

[53] Gupta, R., Béchara, H., El Maarouf, I., & Orasan, C. (2014, August). UoW: NLP techniques developed at the University of Wolverhampton for Semantic Similarity and Textual Entailment. In 8th Int. Workshop on Semantic Evaluation (SemEval'14) (pp. 785-789).

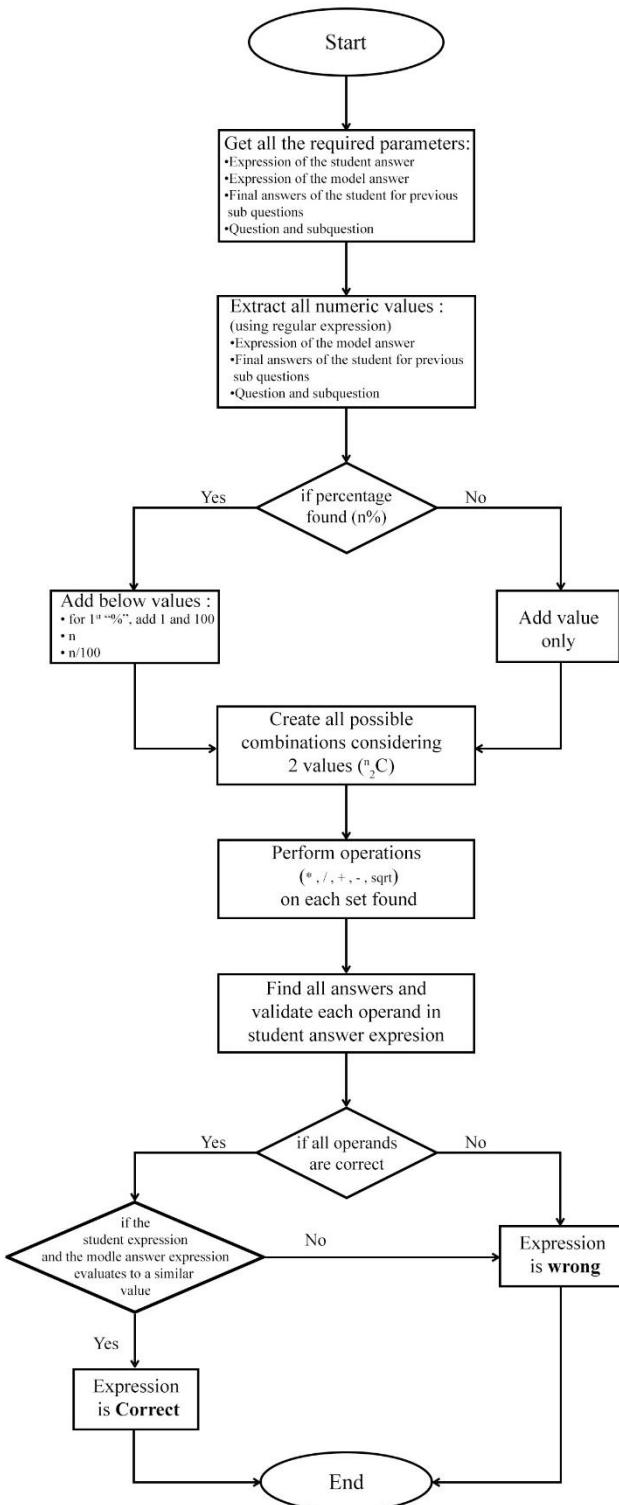
## Appendix A: Flow chart for answer expression evaluation



## Appendix B: Flow chart for final answer evaluation



## Appendix C: Flow chart for Expression validation



## Appendix D: Computer Representation of the Marking Rubric, Question, Unit Categorization and the Answer (XML Documents)

```

<?xml version="1.0" encoding="UTF-8"?>
<rubric>
    <type>InterestCalculation</type>
    <sectionid>1</sectionid>
    <question id="q01" totalMarks="10">
        <sub_question id="q01-01" totalMarks="1" isProof="true">
            <mark_set id="1">
                <data required="true" isFinal="false" marks="1">
                    <phrase>Total amount spent</phrase>
                    <math_expression unitCompulsory="false" >
                        <mn>600000</mn>
                        <mo>*</mo>
                        <mn>30</mn>
                        <mo>/</mo>
                        <mn>100</mn>
                    </math_expression>
                </data>
                <data required="true" isFinal="true" penalty="1">
                    <value unitCompulsory="true" >
                        <preunit>s01-01</preunit>
                        <val>180000</val>
                    </value>
                </data>
            </mark_set>
        </sub_question>
        <sub_question id="q01-02" totalMarks="2" isProof="true">
        <sub_question id="q01-03" totalMarks="2" isProof="false">
        <sub_question id="q01-04" totalMarks="2" isProof="false">
        <sub_question id="q01-05" totalMarks="3" isProof="false">
    </question>
</rubric>

```

Figure D.1 XML representations of rubric document

```

<?xml version="1.0" encoding="UTF-8"?>
<units>
    <type>Units</type>
    <local_units id="1">
        <type>Mathematics</type>
        <section id="s01" >
            <name>Currency</name>
            <unit_set id="s01-01">
                <data>ශ්‍රී ලංකා රුපේ</data>
                <data>අරුන්දල</data>
                <data>Rupee</data>
                <data>Rs</data>
                <data>LKR</data>
                <data>Sri Lankan Rupee</data>
            </unit_set>
            <unit_set id="s01-02">
        </section>
        <section id="s02" >
    </local_units>
</units>

```

Figure D.2 XML representations of unit categorization

```

<?xml version="1.0" encoding="UTF-8"?>
<answer_script>
  <type>AnswerScript</type>
  <student id="RU/E/2010/070">
    <question id="q01" >
      <manualGradingMarks>10</manualGradingMarks>
      <sub_question id="q01-01" >
      <sub_question id="q01-02" >
      <sub_question id="q01-03" >
      <sub_question id="q01-04" >
      <sub_question id="q01-05" >
        <manualGradingMarks_sub>3</manualGradingMarks_sub>
        <answer>Total amount at the end of the second year=420000*1.08^2</answer>
        <answer>=61489888</answer>
      </sub_question>
    </question>
  </answer_script>

```

Figure D.3 XML representations of student answer

## Appendix E: Example word problems in Sinhala language

<p>පුද්ගලයෙක් තමා සතු රු .420000 ස්ථාවර ගිණුමක තැන්පත් කරයි. වාර්ෂික වැල් පොලී අනුපාතිකය 8% ක් නම් මුල් වසර දෙක අවසානයේදී ගිණුමෙහි ඇති මුළු මුදල ගණනය කරන්න.</p>	
පලමු වසර අවසානයේ පොලීය	= $420000 * 8 / 100$ = Rs.33600
දෙවන වසර අවසානයේ පොලීය	= $(420000 + 33600) * 8 / 100$ = Rs.36288
දෙවන වසර අවසානයේ මුළු මුදල	= $420000 + 33600 + 36288$ = Rs.489888

Figure 1 Numerical word problem and its sample answer

<p>පත්‍රලේඛ අරය <math>r</math> cm ද උස 12cm ද වන තුනී කුහර කේතුවක් සම්පූර්ණයෙන්ම ජලයෙන් පුරවා පැත්තක දිග 8cm වන සමවතුරසාකාර පත්‍රලක් සහිත භාජනයකට වත් කරනු ලැබේ. කේතුවේ ජල පරිමාව <math>r</math> ඇසුරින් සොයන්න.</p>	
කේතුවේ ජල පරිමාව	= $1/3 * \pi * r^2 * h$ = $1/3 * \pi * r^2 * 12$ = $4 * \pi * r^2$

Figure 2 Algebraic word problem and its sample answer

## Appendix F: Sample word set in Sinhala-Sinhala lexical database

