# **CHAPTER SIX**

# 6.1 Results

Several runs were made. The following results presented were obtained by running the program for 325 generations.

The coefficients used in fitness function were;

| Parameter | Coefficient | Declaration                              |
|-----------|-------------|--|
| Load      | 0.4         | giving the idea of the amount            |
| NoLines   | 0.35        | Over loaded giving the idea of number of |
| TC        |             | Non – over loading lines                 |
|           | 0.3         | Total cost                               |
| L_F       | 0.3         | Line fitness                             |
| n         | 0.15        | Number of under loaded lines             |

The average program run time for 325 generations have been around 9 minutes.

These are the results obtained for 10 runs of program. Summery has been tabulated;

| No | Tcost | Nlines | TLineLength | Nover     | Avg<br>OverLoad | Nunder    | Avg        |
|----|-------|--------|-------------|-----------|-----------------|-----------|------------|
|    |       |        |             | LoadLines | %               | LoadLines | UnderLoad% |
| 1  | 3065  | 9      | 510         | 4         | 170.51          | 2         | 14         |
| 2  | 3175  | 8      | 520         | 3         | 144.17          | 2         | 11.48      |
| 3  | 3175  | 8      | 520         | 3         | 144.18          | 2         | 15.27      |
| 4  | 3730  | 10     | 620         | 2         | 133             | 3         | 11.86      |
| 5  | 5445  | 13     | 890         | 2         | 135.65          | 6         | 15.62      |
| 6  | 5540  | 13     | 890         | 0         | 0               | 5         | 9.89       |
| 7  | 5720  | 14     | 980         | 2         | 115.43          | 6         | 13.15      |
| 8  | 6250  | 15     | 1090        | 0         | 0               | 6         | 13.74      |
| 9  | 6330  | 15     | 1090        | 1         | 111.8           | 7         | 14.16      |
| 10 | 6475  | 15     | 1090        | 1         | 119.37          | 5         | 11.29      |

Using this type of result table designer can select suitable solution according to his requirement.

Detailed No 1 result;

| From | 10 | Line Type      |
|------|----|----------------|
| 1    | 2  | Lynx           |
| 1    | 5  | Lynx           |
| 2    | 3  | 350 Oil Filled |
| 2    | 4  | 300 XLPE       |
| 2    | 5  | Lynx           |
| 2    | 6  | 1xZebra        |
| 3    | 5  | Lynx           |
| 3    | 6  | Bear           |
| 4    | 6  | 300 XLPE       |

Total cost (in millions) = 3065 Total number of lines = 9 Total Line length (in km) = 510

# System Summary

| How many?        |    | How much?                    | P (MW)                                       | Q (MVAR)               |
|------------------|----|------------------------------|--|------------------------|
| Buses            | 6  | Total Gen Capacity           | 1110.0                                       | -900.0 to +900.0       |
| Generators       | 3  | On-line Capacity             | 1110.0                                       | -900.0 to +900.0       |
| Committed Gens   | 3  | Generation (current)         | 770.0  | 118.5                  |
| Loads            | 5  | Load                         | 770.0  | 0.0                    |
| Branches         | 9  | Losses $(I^2 * Z)$           | 0.00   | 118.53                 |
| Transformers     | 0  | Branch Charging (inj)        | -  | 0.0                    |
| Areas            | 1  | Shunt (inj)                  | 0.0  | 0.0                    |
| Inter-ties       | 0  | Total Inter-tie Flow Minimum | 0.0<br>Moratuwa, s<br>neses & Disse<br>ac.lk | 0. <b>0</b><br>Maximum |
| Voltage Magnitud | de | 0.986 p.u. @ bu              | s 4 1.0                                      | 000 n.u. @ bus 1       |

| Voltage Magnitude | 0.986 p.u. @ bus 4 | 1.000 p.u. @ bus 1    |
|-------------------|--------------------|-----------------------|
| Voltage Angle     | -1.77 deg @ bus 5  | 14.85 deg @ bus 6     |
| P Losses (I^2*R)  | •                  | 0.00 MW @ line 1-2    |
| Q Losses (I^2*X)  | -                  | 33.74 MVAR @ line 2-6 |

#### **Bus Data**

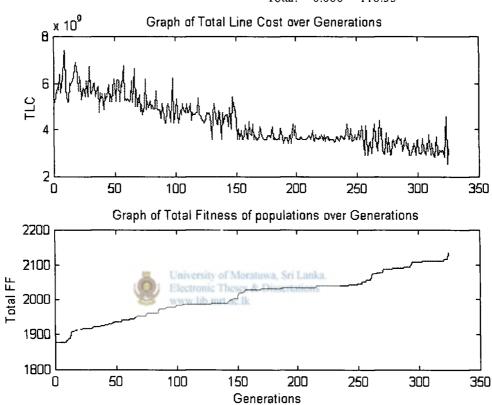
| Bus Voltage |        | Gene       | eration | Loa      | Load   |          |
|-------------|--------|------------|---------|----------|--------|----------|
| #           | Mag(pu | ) Ang(deg) | P (MW)  | Q (MVAR) | P (MW) | Q (MVAR) |
|             |        |            |         |          |        |          |
| 1           | 1.000  | 0.000      | 70.00   | 13.48    | 90.00  | 0.00     |
| 2           | 0.993  | 3.715      | -       | -        | 240.00 | 0.00     |
| 3           | 1.000  | 6.992      | 300.00  | 50.62    | 40.00  | 0.00     |
| 4           | 0.986  | 3.409      | -       | -        | 160.00 | 0.00     |
| 5           | 0.992  | -1.770     | -       | -        | 240.00 | 0.00     |
| 6           | 1.000  | 14.851     | 400.00  | 54.43    | -      | -        |
|             |        |            |         |          |        |          |
|             |        | Total:     | 770.00  | 118.53   | 770.00 | 0.00     |

#### **Branch Data**

| From<br>Bus | To<br>Bus |        | us Injection<br>Q (MVAR) | To Bus I<br>P (MW) | Injection<br>Q (MVAR) | Loss (I^<br>P (MW) | 2 * Z)<br>Q (MVAR) |
|-------------|-----------|--------|--------------------------|--------------------|-----------------------|--------------------|--------------------|
| 1           | <br>2     | -46.65 | 6.31                     | 46.65              | -3.25                 | 0.000              | 3.06               |
| 1           | 2         | -40.03 | 0.31                     | 40.03              | -3.23                 | 0.000              | 3.06               |

| 1 | 5 | 26.65   | 7.17   | -26.65  | -6.29 | 0.000 | 0.88  |
|---|---|---------|--------|---------|-------|-------|-------|
| 2 | 3 | -199.23 | -17.39 | 199.23  | 28.94 | 0.000 | 11.55 |
| 2 | 4 | 3.50    | 4.80   | -3.50   | -4.75 | 0.000 | 0.05  |
| 2 | 5 | 81.93   | 4.92   | -81.93  | 2.93  | 0.000 | 7.85  |
| 2 | 6 | -172.84 | 10.92  | 172.84  | 22.81 | 0.000 | 33.74 |
| 3 | 5 | 131.43  | 16.83  | -131.43 | 3.36  | 0.000 | 20.19 |
| 3 | 6 | -70.66  | 4.85   | 70.66   | 4.85  | 0.000 | 9.71  |
| 4 | 6 | -156.50 | 4.75   | 156.50  | 26.77 | 0.000 | 31.51 |
|   |   |         |        |         |       |       |       |

Total: 0.000 118.53



# Detailed No 2 result;

| From | To | Line Type       |
|------|----|-----------------|
| 1    | 2  | 300 XLPE        |
| 2    | 3  | Lynx            |
| 2    | 4  | 300 XLPE        |
| 2    | 5  | Lynx            |
| 3    | 4  | 1x <b>G</b> oat |
| 3    | 5  | Bear            |
| 4    | 6  | 1xZebra         |
| 5    | 6  | Lynx            |

Total cost (in millions) = 3175 Total number of lines = 8 Total Line length (in km) = 520

# System Summary

| How many?      |   | How much?             | P (MW) | Q (MVAR)         |
|----------------|---|-----------------------|--------|------------------|
|                | - |                       |        |                  |
| Buses          | 6 | Total Gen Capacity    | 1110.0 | -900.0 to +900.0 |
| Generators     | 3 | On-line Capacity      | 1110.0 | -900.0 to +900.0 |
| Committed Gens | 3 | Generation (current)  | 770.0  | 176.2            |
| Loads          | 5 | Load                  | 770.0  | 0.0              |
| Branches       | 8 | Losses (I^2 * Z)      | 0.0    | 176.23           |
| Transformers   | 0 | Branch Charging (inj) | -      | 0.0              |
| Areas          | 1 | Shunt (inj)           | 0.0    | 0.0              |
| Inter-ties     | 0 | Total Inter-tie Flow  | 0.0    | 0.0              |

|                              | Minimum            | Maximum               |  |  |
|------------------------------|--------------------|-----------------------|--|--|
| Voltage Magnitude            | 0.974 p.u. @ bus 4 | 1.000 p.u. @ bus 1    |  |  |
| Voltage Angle                | 0.00 deg @ bus 1   | 24.87 deg @ bus 6     |  |  |
| P Losses (I <sup>2</sup> *R) | -                  | 0.00 MW @ line 1-2    |  |  |
| Q Losses (I^2*X)             | -                  | 63.99 MVAR @ line 4-6 |  |  |

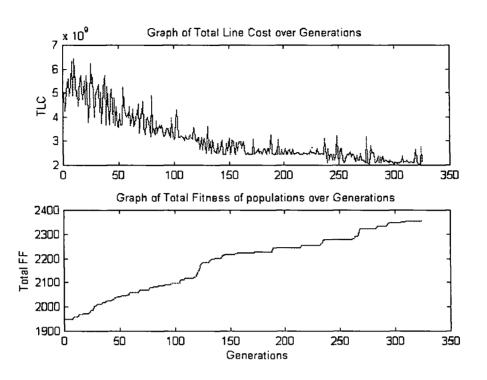
1

# Bus Data

| Bu | s Volt | age G      | eneration | Load            |        |          |
|----|--------|------------|-----------|-----------------|--------|----------|
| #  | Mag(pu | ) Ang(deg) | P (MW)    | Q (MVAR)        | P (MW) | Q (MVAR) |
|    |        |            |           |                 |        |          |
| 1  | 1.000  | 0.000      | 70.00     | 12.60           | 90.00  | 0.00     |
| 2  | 0.982  | 1.751      | -         | -               | 240.00 | 0.00     |
| 3  | 1.000  | 11.136     | 300.00    | 66.67           | 40.00  | 0.00     |
| 4  | 0.974  | 9.421      | no.       | University of a | 160.00 | 0.00     |
| 5  | 0.976  | 4.212      |           | www lib met a   | 240.00 | 0.00     |
| 6  | 1.000  | 24.866     | 400.00    | 96.96           | -      | -        |
|    |        |            |           |                 |        |          |
|    | To     | tal:       | 770.00    | 176.23          | 770.00 | 0.00     |

# |Branch Data

| From<br>Bus | To<br>Bus | From Bus<br>P (MW) | Injection<br>Q (MVAR) | To Bus<br>P (MW) | Injection | Loss (I^2 | •        |
|-------------|-----------|--------------------|-----------------------|------------------|-----------|-----------|----------|
| Dus         | Dus       | r (MW)             | Q (MVAK)              | r (IVI W)        | Q (MVAR)  | P (MW)    | Q (MVAR) |
|             |           |                    |                       |                  |           |           |          |
| 1           | 2         | -20.00             | 12.60                 | 20.00            | -11.77    | 0.000     | 0.84     |
| 2           | 3         | -139.17            | -4.32                 | 139.17           | 27.46     | 0.000     | 23.14    |
| 2           | 4         | -85.06             | 10.63                 | 85.06            | 0.81      | 0.000     | 11.44    |
| 2           | 5         | -35.77             | 5.46                  | 35.77            | -3.90     | 0.000     | 1.56     |
| 3           | 4         | 11.37              | 10.31                 | -11.37           | -9.70     | 0.000     | 0.60     |
| 3           | 5         | 109.45             | 28.89                 | -109.45          | -15.12    | 0.000     | 13.78    |
| 4           | 6         | -233.69            | 8.89                  | 233.69           | 55.09     | 0.000     | 63.99    |
| 5           | 6         | -166.31            | 19.01                 | 166.31           | 41.87     | 0.000     | 60.89    |
|             |           |                    |                       |                  |           |           |          |
|             |           |                    |                       |                  | Total:    | 0.000     | 176.23   |



#### Detailed No 3 result;

| From | To | Line Type 💻 | University of Moratuwa, Sri Lanka. |
|------|----|-------------|------------------------------------|
| 1    | 2  | 300 XLPE    | Electronic Theses & Dissertations  |
| 2    | 3  | Lynx        | www.lib.mrt.ac.lk                  |
| 2    | 4  | 300 XLPE    |                                    |
| 2    | 5  | Lynx        |                                    |
| 3    | 4  | 1xGoat      |                                    |
| 3    | 5  | Bear        |                                    |
| 4    | 6  | 1xZebra     |                                    |

Total cost (in millions) = 3175 Total number of lines = 8 Total Line length (in km) = 520

Lynx

#### **System Summary**

6

5

| How many?      |   | How much?             | P (MW) | Q (MVAR)         |
|----------------|---|-----------------------|--------|------------------|
| Buses          | 6 | Total Gen Capacity    | 1110.0 | -900.0 to +900.0 |
| Generators     | 3 | On-line Capacity      | 1110.0 | -900.0 to +900.0 |
| Committed Gens | 3 | Generation (current)  | 770.0  | 176.2            |
| Loads          | 5 | Load                  | 770.0  | 0.0              |
| Branches       | 8 | Losses $(I^2 * Z)$    | 0.00   | 176.23           |
| Transformers   | 0 | Branch Charging (inj) | -      | 0.0              |
| Areas          | 1 | Shunt (inj)           | 0.0    | 0.0              |
| Inter-ties     | 0 | Total Inter-tie Flow  | 0.0    | 0.0              |

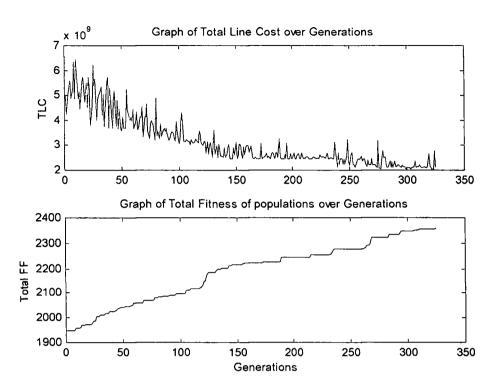
|  | Minimum                                | Maximum  |
|--|--|--|
| Voltage Magnitude<br>Voltage Angle<br>P Losses (I^2*R)<br>Q Losses (I^2*X) | 0.974 p.u. @ bus 4<br>0.00 deg @ bus 1 | 1.000 p.u. @ bus 1<br>24.87 deg @ bus 6<br>0.00 MW @ line 1-2<br>63.99 MVAR @ line 4-6 |
|  |  |  |

# **Bus Data**

| Bus | Voltage |          | Gene   | ration   | Load   |          |
|-----|---------|----------|--------|----------|--------|----------|
| #   | Mag(pu) | Ang(deg) | P (MW) | Q (MVAR) | P (MW) | Q (MVAR) |
|     |         |          |        |          |        |          |
| 1   | 1.000   | 0.000    | 70.00  | 12.60    | 90.00  | 0.00     |
| 2   | 0.982   | 1.751    | -      | -        | 240.00 | 0.00     |
| 3   | 1.000   | 11.136   | 300.00 | 66.67    | 40.00  | 0.00     |
| 4   | 0.974   | 9.421    | -      | -        | 160.00 | 0.00     |
| 5   | 0.976   | 4.212    | -      | -        | 240.00 | 0.00     |
| 6   | 1.000   | 24.866   | 400.00 | 96.96    | -      | -        |
|     |         |          |        |          |        |          |
|     |         | Total:   | 770.00 | 176.23   | 770.00 | 0.00     |

# **Branch Data**

| From<br>Bus | To<br>Bus | From Bo<br>P (MW) | us Injection<br>Q (MVAF | To Bus I | Injection<br>Q (MVAR) | Loss (I^:<br>P (MW) | 2 * Z)<br>Q (MVAR) |
|-------------|-----------|-------------------|-------------------------|----------|-----------------------|---------------------|--------------------|
| 1           | 2         | -20.00            | 12.60                   | 20.00    | -11.77                | 0.000               | 0.84               |
| 2           | 3         | -139.17           | -4.32                   | 139.17   | 27.46                 | 0.000               | 23.14              |
| 2           | 4         | -85.06            | 10.63                   | 85.06    | 0.81                  | 0.000               | 11.44              |
| 2           | 5         | -35.77            | 5.46                    | 35.77    | -3.90                 | 0.000               | 1.56               |
| 3           | 4         | 11.37             | 10.31                   | -11.37   | -9.70                 | 0.000               | 0.60               |
| 3           | 5         | 109.45            | 28.89                   | -109.45  | -15.12                | 0.000               | 13.78              |
| 4           | 6         | -233.69           | 8.89                    | 233.69   | 55.09                 | 0.000               | 63.99              |
| 5           | 6         | -166.31           | 19.01                   | 166.31   | 41.87                 | 0.000               | 60.89              |
|             |           |                   |                         |          |                       |                     |                    |
|             |           |                   |                         |          | Total:                | 0.000               | 176.23             |



#### Detailed No 4 result;

| From | To | Line Type      | University of Moratuwa, Sri Lanka.<br>Electronic Theses & Dissertations |
|------|----|----------------|---|
| 1    | 2  | Lynx           | www.lib.mrt.ac.lk   |
| 1    | 5  | 350 Oil Filled |   |
| 2    | 3  | 300 XLPE       |   |
| 2    | 4  | 350 Oil Filled |   |
| 2    | 5  | 300 XLPE       |   |
| 2    | 6  | Lynx           |   |
| 3    | 4  | 300 XLPE       |   |
| 3    | 5  | 300 XLPE       |   |
| 4    | 6  | 300 XLPE       |   |
| 5    | 6  | Lynx           |   |

Total cost (in millions) = 3730 Total number of lines = 10 Total Line length (in km) = 620

#### **System Summary**

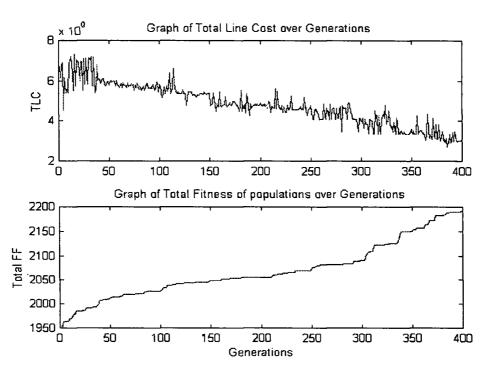
| How many?      | _  | How much?             | P (MW) | Q (MVAR)         |
|----------------|----|-----------------------|--------|------------------|
| Buses          | 6  | Total Gen Capacity    | 1110.0 | -900.0 to +900.0 |
| Generators     | 3  | On-line Capacity      | 1110.0 | -900.0 to +900.0 |
| Committed Gens | 3  | Generation (current)  | 770.0  | 112.9            |
| Loads          | 5  | Load                  | 770.0  | 0.0              |
| Branches       | 10 | Losses $(I^2 * Z)$    | 0.00   | 112.90           |
| Transformers   | 0  | Branch Charging (inj) | · -    | 0.0              |
| Areas          | 1  | Shunt (inj)           | 0.0    | 0.0              |
| Inter-ties     | 0  | Total Inter-tie Flow  | 0.0    | 0.0              |

1

|  | I  |  |  | inimum M   |                                     | <b>I</b> aximum  |   |
|--|--|--|--|--|-------------------------------------|--|---|
| Voltage Magnitude<br>Voltage Angle<br>P Losses (1^2*R)<br>Q Losses (1^2*X) |  |  |  | •  |                                     | 1.000 p.u. @ bus 1<br>12.14 deg @ bus 6<br>0.00 MW @ line 1-2<br>29.65 MVAR @ line 2-6 |   |
| Bus I  | Data   |  |  |  | ţ                                   |  |   |
| Bus<br>#   |  | Voltage<br>pu) Ang(d   |  | eration<br>) Q (MVA  | Lo<br>AR) P(MW                      |  | AR)   |
| 1<br>2<br>3<br>4<br>5<br>6   | 1.00<br>0.99<br>1.00<br>0.99<br>0.99           | 01 1.512<br>00 8.651<br>00 1.953<br>05 0.017   | 70.00<br>-<br>300.00<br>-<br>-<br>2 400.00                                       | 23.99<br>32.50<br>56.41  | 240.00<br>40.00<br>160.00<br>240.00 | 0.00<br>0.00<br>0.00<br>0.00<br>0.00   |   |
|  |  | Tota   | al: 770.00   | 112.90   | 770.00                              | 0.00   |   |
| Bran   | ch Da  | ta   |  |  | 1                                   |  |   |
| From<br>Bus  | To<br>Bus                                      |  | us Injection<br>Q (MVAR)   |  | njection<br>Q (MVAR)                | Loss (I<br>P (MW)  | ^2 * Z)<br>Q (MVAR)   |
| 1<br>1<br>2<br>2<br>2<br>2<br>2<br>2<br>3<br>3<br>4<br>5                   | 2<br>5<br>3<br>4<br>5<br>6<br>4<br>5<br>6<br>6 | -18.95<br>-1.05<br>-98.52<br>-22.06<br>20.58<br>-158.95<br>41.98<br>119.50<br>-140.08<br>-100.97 | 6.82<br>17.17<br>-1.04<br>3.37<br>-3.04<br>6.97<br>6.17<br>12.94<br>4.41<br>8.37 | 18.95<br>1.05<br>98.52<br>22.06<br>-20.58<br>158.95<br>-41.98<br>-119.50<br>140.08<br>100.97 | -17.09                              | 0.000<br>0.000<br>0.000<br>0.000<br>0.000<br>0.000<br>0.000<br>0.000<br>0.000          | 0.56<br>0.08<br>12.36<br>0.17<br>0.55<br>29.65<br>4.95<br>18.06<br>25.06<br>21.46 |

Total: 0.000

112.90



Detailed No 5 result;

| From | To | Line Type  |    |
|------|----|--|----|
| 1    | 2  | 300 XLPE University of Moratuwa, Sri Lanks       | a. |
| 1    | 3  | 350 Oil Filled Electronic Theses & Dissertations |    |
| 1    | 5  | Lynx www.lib.mrt.ac.lk                           |    |
| 2    | 3  | Lynx   |    |
| 2    | 4  | Lynx   |    |
| 2    | 5  | 300 XLPE   |    |
| 2    | 6  | 300 XLPE   |    |
| 3    | 4  | 300 XLPE   |    |
| 3    | 5  | Lynx   |    |
| 3    | 6  | 300 XLPE   |    |
| 4    | 5  | 300 XLPE   |    |
| 4    | 6  | 1 x Zebra  |    |
| 5    | 6  | 300 XLPE   |    |

Total cost (in millions) = 5445 Total number of lines = 13 Total Line length (in km) = 890

#### System Summary

| How many?      |    | How much?             | P (MW) | Q (MVAR)         |  |
|----------------|----|-----------------------|--------|------------------|--|
|                | -  |                       |        |                  |  |
| Buses          | 6  | Total Gen Capacity    | 1110.0 | -900.0 to +900.0 |  |
| Generators     | 3  | On-line Capacity      | 1110.0 | -900.0 to +900.0 |  |
| Committed Gens | 3  | Generation (current)  | 770.0  | 93.9             |  |
| Loads          | 5  | Load                  | 770.0  | 0.0              |  |
| Branches       | 13 | Losses $(I^2 * Z)$    | 0.00   | 93.92            |  |
| Transformers   | 0  | Branch Charging (inj) | -      | 0.0              |  |



| Areas      | 1 | Shunt (inj)          | 0.0 | 0.0 |
|------------|---|----------------------|-----|-----|
| Inter-ties | 0 | Total Inter-tie Flow | 0.0 | 0.0 |

|  | Minimum                                 | Maximum   |  |  |
|--|---|---|--|--|
| Voltage Magnitude<br>Voltage Angle<br>P Losses (1^2*R)<br>Q Losses (1^2*X) | 0.991 p.u. @ bus 4<br>-3.33 deg @ bus 5 | 1.000 p.u. @ bus 1<br>7.32 deg @ bus 6<br>0.00 MW @ line 1-2<br>23.97 MVAR @ line 4-6 |  |  |

1

1

Total: 0.000

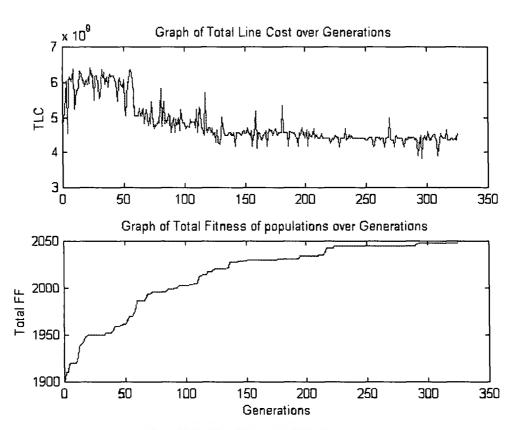
93.92

# Bus Data

| Bus | Voltage |          | Gene   | eration  | Load   |          |
|-----|---------|----------|--------|----------|--------|----------|
| #   | Mag(pu) | Ang(deg) | P (MW) | Q (MVAR) | P (MW) | Q (MVAR) |
|     |         |          |        |          |        |          |
| 1   | 1.000   | 0.000    | 70.00  | 15.29    | 90.00  | 0.00     |
| 2   | 0.993   | -2.573   | -      | -        | 240.00 | 0.00     |
| 3   | 1.000   | 2.609    | 300.00 | 28.77    | 40.00  | 0.00     |
| 4   | 0.991   | -2.067   | -      | -        | 160.00 | 0.00     |
| 5   | 0.993   | -3.327   | -      | -        | 240.00 | 0.00     |
| 6   | 1.000   | 7.318    | 400.00 | 49.86    | -      | -        |
|     |         |          |        |          |        |          |
|     |         | Total:   | 770.00 | 93.92    | 770.00 | 0.00     |

# **Branch Data**

| From | To  | From Bus           | Injection | To Bus         | Injection      | Loss (I' | 2 * Z)   |
|------|-----|--------------------|-----------|----------------|----------------|----------|----------|
| Bus  | Bus | P (MW)             | Q (MVA    | R) P(MW)       | Q (MVAR        | ) P (MW) | Q (MVAR) |
|      |     |                    | 7007      | Electronic The | es & Discourts | ions     |          |
| 1    | 2   | 29.71              | 5.55      | -29.71         | -4.18          | 0.000    | 1.37     |
| 1    | 3   | -99.83             | 2.27      | 99.83          | 2.27           | 0.000    | 4.55     |
| 1    | 5   | 50.12              | 7.47      | -50.12         | -4.51          | 0.000    | 2.95     |
| 2    | 3   | <del>-</del> 77.97 | -2.79     | 77.97          | 9.89           | 0.000    | 7.10     |
| 2    | 4   | -6.30              | 1.23      | 6.30           | -1.17          | 0.000    | 0.06     |
| 2    | 5   | 10.38              | -0.25     | -10.38         | 0.39           | 0.000    | 0.14     |
| 2    | 6   | -136.41            | 5.99      | 136.41         | 17.66          | 0.000    | 23.65    |
| 3    | 4   | 29.38              | 4.47      | -29.38         | -2.04          | 0.000    | 2.43     |
| 3    | 5   | 89.31              | 10.64     | -89.31         | -1.34          | 0.000    | 9.30     |
| 3    | 6   | -36.48             | 1.50      | 36.48          | 1.50           | 0.000    | 3.00     |
| 4    | 5   | 8.66               | -0.73     | -8.66          | 0.92           | 0.000    | 0.19     |
| 4    | 6   | -145.58            | 3.93      | 145.58         | 20.04          | 0.000    | 23.97    |
| 5    | 6   | -81.53             | 4.54      | 81.53          | 10.67          | 0.000    | 15.21    |
|      |     |                    |           |                |                |          |          |



Detailed No 6 result;

To

From

Line Type

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| 1 | 2 | 1xZebra        |
|---|---|----------------|
| 1 | 3 | 300 XLPE       |
| 1 | 5 | Lynx           |
| 2 | 3 | 300 XLPE       |
| 2 | 4 | Lynx           |
| 2 | 5 | 350 Oil Filled |
| 2 | 6 | 2xZebra        |
| 3 | 4 | 300 XLPE       |
| 3 | 5 | 300 XLPE       |
| 3 | 6 | 300 XLPE       |
| 4 | 5 | Lynx           |
| 4 | 6 | 1xGoat         |
| 5 | 6 | 300 XLPE       |

Total cost (in millions) = 5540 Total number of lines = 13 Total Line length (in km) = 890

#### System Summary

| How many?  |   | How much?          | P (MW) | Q (MVAR)         |  |
|------------|---|--------------------|--------|------------------|--|
|            |   |                    |        |                  |  |
| Buses      | 6 | Total Gen Capacity | 1110.0 | -900.0 to +900.0 |  |
| Generators | 3 | On-line Capacity   | 1110.0 | -900.0 to +900.0 |  |

| Committed Gens   | 3  | Generation (current)                    | 770.0                 | 94.8  |
|--|----|---|-----------------------|-------|
| Loads  | 5  | Load                                    | 770.0                 | 0.0   |
| Branches   | 13 | Losses (I^2 * Z)                        | 0.00                  | 94.84 |
| Transformers   | 0  | Branch Charging (inj)                   | -                     | 0.0   |
| Areas  | 1  | Shunt (inj)                             | 0.0                   | 0.0   |
| Inter-ties   | 0  | Total Inter-tie Flow                    | 0.0                   | 0.0   |
|  |    | Minimum                                 | Maximum               |       |
| Voltage Magnitude<br>Voltage Angle<br>P Losses (I^2*R)<br>Q Losses (I^2*X) |    | 0.991 p.u. @ bus 4<br>-1.38 deg @ bus 5 | 1.000 p.u<br>8.28 deg | _     |

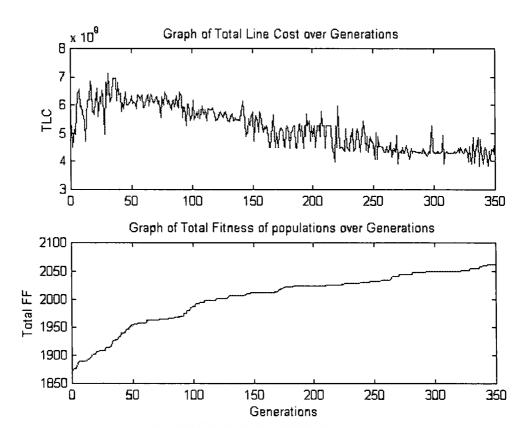
#### **Bus Data**

| Bus | Voltage |            | Generation |          | Load   |          |
|-----|---------|------------|------------|----------|--------|----------|
| #   | Mag(pu  | ) Ang(deg) | P (MW)     | Q (MVAR) | P (MW) | Q (MVAR) |
|     |         |            |            |          |        |          |
| 1   | 1.000   | 0.000      | 70.00      | 14.40    | 90.00  | 0.00     |
| 2   | 0.993   | -0.734     | -          | -        | 240.00 | 0.00     |
| 3   | 1.000   | 5.787      | 300.00     | 31.05    | 40.00  | 0.00     |
| 4   | 0.991   | -0.505     | -          | -        | 160.00 | 0.00     |
| 5   | 0.993   | -1.385     | -          | -        | 240.00 | 0.00     |
| 6   | 1.000   | 8.277      | 400.00     | 49.38    | -      | -        |
|     |         |            |            |          |        |          |
|     |         | Total:     | 770.00     | 94 84    | 770.00 | 0.00     |

|

| Branc | ch Data |         | UI UI        | liversity of a | vioratuwa, Sri L | anka.    |          |
|-------|---------|---------|--------------|----------------|------------------|----------|----------|
| From  | To      | From B  | us Injection | To Bus         | Injection        | Loss (I^ | 2. * Z)  |
| Bus   | Bus     | P (MW)  | Q (MVAR)     | P (MW)         | Q (MVAR)         | P (MW)   | Q (MVAR) |
|       |         |         |              |                |                  |          |          |
| 1     | 2       | 9.55    | 5.52         | -9.55          | -5.36            | 0.000    | 0.16     |
| 1     | 3       | -50.42  | 2.55         | 50.42          | 2.55             | 0.000    | 5.10     |
| 1     | 5       | 20.87   | 6.33         | -20.87         | -5.79            | 0.000    | 0.55     |
| 2     | 3       | -90.20  | -0.63        | 90.20          | 10.95            | 0.000    | 10.32    |
| 2     | 4       | -2.85   | 1.00         | 2.85           | -0.99            | 0.000    | 0.01     |
| 2     | 5       | 39.30   | -0.74        | -39.30         | 1.18             | 0.000    | 0.45     |
| 2     | 6       | -176.70 | 5.72         | 176.70         | 22.18            | 0.000    | 27.91    |
| 3     | 4       | 39.51   | 5.32         | -39.51         | -0.95            | 0.000    | 4.37     |
| 3     | 5       | 99.18   | 11.81        | -99.18         | 0.66             | 0.000    | 12.47    |
| 3     | 6       | -19.31  | 0.42         | 19.31          | 0.42             | 0.000    | 0.84     |
| 4     | 5       | 6.57    | -0.67        | -6.57          | 0.77             | 0.000    | 0.10     |
| 4     | 6       | -129.92 | 2.61         | 129.92         | 17.41            | 0.000    | 20.02    |
| 5     | 6       | -74.07  | 3.17         | 74.07          | 9.37             | 0.000    | 12.54    |
|       |         |         |              |                |                  |          |          |

Total: 0.000 94.84



Detailed No 7 result;



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| From | To | Line Type      |
|------|----|----------------|
| 1    | 2  | 300 XLPE       |
| 1    | 3  | Lynx           |
| 1    | 4  | 300 XLPE       |
| 1    | 5  | l x Zebra      |
| 1    | 6  | Lynx           |
| 2    | 3  | 1 x Zebra      |
| 2    | 4  | Lynx           |
| 2    | 5  | 350 Oil Filled |
| 2    | 6  | Lynx           |
| 3    | 5  | 300 XLPE       |
| 3    | 6  | Lynx           |
| 4    | 5  | 300 XLPE       |
| 4    | 6  | 300 XLPE       |
| 5    | 6  | 300 XLPE       |

Total cost (in millions) = 5720 Total number of lines = 14 Total Line length (in km) = 980

#### System Summary

| How many?      |    | How much?             | P (MW) | Q (MVAR)         |
|----------------|----|-----------------------|--------|------------------|
|                | -  |                       |        |                  |
| Buses          | 6  | Total Gen Capacity    | 1110.0 | -900.0 to +900.0 |
| Generators     | 3  | On-line Capacity      | 1110.0 | -900.0 to +900.0 |
| Committed Gens | 3  | Generation (current)  | 770.0  | 99.7             |
| Loads          | 5  | Load                  | 770.0  | 0.0              |
| Branches       | 14 | Losses (I^2 * Z)      | 0.00   | 99.69            |
| Transformers   | 0  | Branch Charging (inj) | -      | 0.0              |
| Areas          | 1  | Shunt (inj)           | 0.0    | 0.0              |
| Inter-ties     | 0  | Total Inter-tie Flow  | 0.0    | 0.0              |

1

|  | Minimum                                      | Maximum   |
|--|--|---|
| Voltage Magnitude<br>Voltage Angle<br>P Losses (I^2*R)<br>Q Losses (I^2*X) | 0.992 p.u. @ bus 4<br>-2.38 deg @ bus 4<br>- | 1.000 p.u. @ bus 1<br>7.20 deg @ bus 6<br>0.00 MW @ line 1-2<br>22.18 MVAR @ line 4-6 |

-

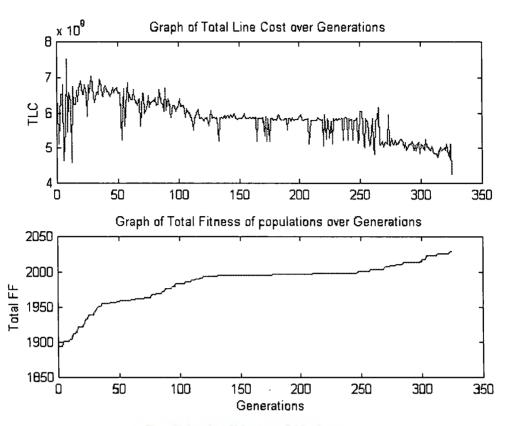
# **Bus Data**

| Bus Voltag | ge       | Gen            | eration          | Load   | d       |
|------------|----------|----------------|------------------|--------|---------|
| # Mag(pu)  | Ang(deg) | P (MW)         | Q (MVAR)         | P (MW) | Q(MVAR) |
|            |          |                |                  |        |         |
| 1 1.000    | 0.000    | 70.00          | 22.50            | 90.00  | 0.00    |
| 2 0.992    | -1.856   | -              | -                | 240.00 | 0.00    |
| 3 1.000    | 5.506    | 300.00         | 29.97            | 40.00  | 0.00    |
| 4 0.992    | -2.384   | ( <b>((</b> )) | lectronic Theses | 160.00 | 0.00    |
| 5 0.993    | -2.273   | 83 W           | ww.lib.mrt.ac.lk | 240.00 | 0.00    |
| 6 1.000    | 7.195    | 400.00         | 47.23            | -      | -       |
|            |          |                |                  |        |         |
|            | Total:   | 770.00         | 99.69            | 770.00 | 0.00    |

#### **Branch Data**

| From | To  | From Bu | s Injection | To Bus I | Injection | Loss (I | ^2 * Z)  |
|------|-----|---------|-------------|----------|-----------|---------|----------|
| Bus  | Bus | P (MW)  | Q (MVAR)    | P (MW)   | Q (MVAR)  |         | Q (MVAR) |
|      |     |         |             |          |           |         |          |
| 1    | 2   | 21.43   | 5.36        | -21.43   | -4.62     | 0.000   | 0.73     |
| 1    | 3   | -52.15  | 2.51        | 52.15    | 2.51      | 0.000   | 5.02     |
| 1    | 4   | 20.63   | 4.55        | -20.63   | -3.65     | 0.000   | 0.89     |
| 1    | 5   | 35.48   | 7.23        | -35.48   | -5.78     | 0.000   | 1.46     |
| 1    | 6   | -45.38  | 2.85        | 45.38    | 2.85      | 0.000   | 5.71     |
| 2    | 3   | -114.58 | 0.65        | 114.58   | 14.14     | 0.000   | 14.79    |
| 2    | 4   | 6.58    | 0.55        | -6.58    | -0.49     | 0.000   | 0.06     |
| 2    | 5   | 25.19   | -0.84       | -25.19   | 1.02      | 0.000   | 0.18     |
| 2    | 6   | -135.77 | 4.26        | 135.77   | 17.28     | 0.000   | 21.54    |
| 3    | 5   | 107.51  | 13.11       | -107.51  | 1.55      | 0.000   | 14.66    |
| 3    | 6   | -14.24  | 0.21        | 14.24    | 0.21      | 0.000   | 0.42     |
| 4    | 5   | -0.76   | -0.39       | 0.76     | 0.39      | 0.000   | 0.00     |
| 4    | 6   | -132.03 | 4.53        | 132.03   | 17.65     | 0.000   | 22.18    |
| 5    | 6   | -72.58  | 2.81        | 72.58    | 9.23      | 0.000   | 12.05    |
|      |     |         |             |          |           |         |          |

Total: 0.000 99.69



Detailed No 8 result;



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| To | Line Type  |
|----|--|
| 2  | 500 XLPE   |
| 3  | 300 XLPE   |
| 4  | 300 XLPE   |
| 5  | 300 XLPE   |
| 6  | Lynx   |
| 3  | Lynx   |
| 4  | 300 XLPE   |
| 5  | 300 XLPE   |
| 6  | 300 XLPE   |
| 4  | Lynx   |
| 5  | 1xZebra  |
| 6  | Lynx   |
| 5  | Lynx   |
| 6  | 300 XLPE   |
| 6  | Lynx   |
|    | 2<br>3<br>4<br>5<br>6<br>3<br>4<br>5<br>6<br>4<br>5<br>6<br>5<br>6<br>5<br>6<br>5<br>6<br>6<br>5<br>6<br>6<br>6<br>6<br>6<br>6 |

Total cost (in millions) = 6250 Total number of lines = 15 Total Line length (in km) = 1090

# System Summary

| How many?      |    | How much?             | P (MW) | Q (MVAR)         |
|----------------|----|-----------------------|--------|------------------|
|                | -  |                       |        |                  |
| Buses          | 6  | Total Gen Capacity    | 1110.0 | -900.0 to +900.0 |
| Generators     | 3  | On-line Capacity      | 1110.0 | -900.0 to +900.0 |
| Committed Gens | 3  | Generation (current)  | 770.0  | 93.4             |
| Loads          | 5  | Load                  | 770.0  | 0.0              |
| Branches       | 15 | Losses (I^2 * Z)      | 0.00   | 93.37            |
| Transformers   | 0  | Branch Charging (inj) | _      | 0.0              |
| Areas          | 1  | Shunt (inj)           | 0.0    | 0.0              |
| Inter-ties     | 0  | Total Inter-tie Flow  | 0.0    | 0.0              |

|  | Minimum                                      | Maximum   |
|--|--|---|
| Voltage Magnitude<br>Voltage Angle<br>P Losses (I^2*R)<br>Q Losses (I^2*X) | 0.994 p.u. @ bus 4<br>-2.09 deg @ bus 5<br>- | 1.000 p.u. @ bus 1<br>7.75 deg @ bus 6<br>0.00 MW @ line 1-2<br>19.45 MVAR @ line 2-6 |

1

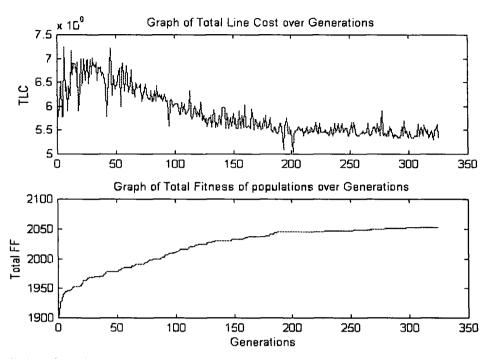
#### **Bus Data**

| Bus Voltage<br># Mag(pu) Ang(deg | Generation P (MW) Q (MVAR) | Load<br>P (MW) Q (MVAR) |
|----------------------------------|----------------------------|-------------------------|
|                                  |                            |                         |
| 1 1.000 0.000                    | 70.00 22.52                | 90.00 0.00              |
| 2 0.995 -1.213                   |                            | 240.00 0.00             |
| 3 1.000 4.896                    | 300.00 28.68               | 40.00 0.00              |
| 4 0.994 -1.014                   | University of Morati       | 160.00 0.00             |
| 5 0.994 -2.089                   | Electronic Theses &        | 240.00 0.00             |
| 6 1.000 7.749                    | 400.00 42.17               |                         |
|                                  |                            |                         |
|                                  | Total: 770.00 93.37        | 770.00 0.00             |

#### **Branch Data**

| From | To  | From Bu | is Injection | To Bus  | Injection | Loss (I^2 | 2 * Z)   |
|------|-----|---------|--------------|---------|-----------|-----------|----------|
| Bus  | Bus |         | Q (MVAR)     |         | Q (MVAR)  | P (MW)    | Q (MVAR) |
|      |     |         |              |         |           |           |          |
| 1    | 2   | 33.75   | 8.61         | -33.75  | -7.85     | 0.000     | 0.76     |
| 1    | 3   | -42.67  | 1.82         | 42.67   | 1.82      | 0.000     | 3.65     |
| 1    | 4   | 8.79    | 3.25         | -8.79   | -3.07     | 0.000     | 0.18     |
| 1    | 5   | 28.98   | 5.53         | -28.98  | -4.44     | 0.000     | 1.09     |
| 1    | 6   | -48.85  | 3.31         | 48.85   | 3.31      | 0.000     | 6.62     |
| 2    | 3   | -92.06  | 0.46         | 92.06   | 9.39      | 0.000     | 9.85     |
| 2    | 4   | -2.29   | 0.80         | 2.29    | -0.79     | 0.000     | 0.01     |
| 2    | 5   | 12.09   | 0.97         | -12.09  | -0.78     | 0.000     | 0.19     |
| 2    | 6   | -123.98 | 5.62         | 123.98  | 13.83     | 0.000     | 19.45    |
| 3    | 4   | 40.44   | 4.60         | -40.44  | -0.40     | 0.000     | 4.19     |
| 3    | 5   | 108.87  | 12.27        | -108.87 | 1.05      | 0.000     | 13.32    |
| 3    | 6   | -24.04  | 0.60         | 24.04   | 0.60      | 0.000     | 1.20     |
| 4    | 5   | 8.05    | 0.03         | -8.05   | 0.12      | 0.000     | 0.15     |
| 4    | 6   | -121.10 | 4.23         | 121.10  | 14.36     | 0.000     | 18.59    |
| 5    | 6   | -82.02  | 4.06         | 82.02   | 10.08     | 0.000     | 14.14    |
|      |     |         |              |         |           |           |          |

Total: 0.000 93.37



Detailed No 9 result;

| From | To | Line Type      |                                    |
|------|----|----------------|------------------------------------|
| 1    | 2  | 350 Oil Filled | University of Moratuwa, Sri Lanka. |
| 1    | 3  |                | Electronic Theses & Dissertations  |
| 1    | 4  |                | www.lib.mrt.ac.lk                  |
| 1    | 5  | Lynx           |                                    |
| 1    | 6  | Lynx           |                                    |
| 2    | 3  | 500 XLPE       |                                    |
| 2    | 4  | 300 XLPE       |                                    |
| 2    | 5  | 300 XLPE       |                                    |
| 2    | 6  | 500 XLPE       |                                    |
| 3    | 4  | Lynx           |                                    |
| 3    | 5  | Lynx           |                                    |
| 3    | 6  | 300 XLPE       |                                    |
| 4    | 5  | Lynx           |                                    |
| 4    | 6  | 1 x Zebra      |                                    |
| 5    | 6  | Lynx           |                                    |

Total cost (in millions) = 6330 Total number of lines = 15 Total Line length (in km) = 1090

#### **System Summary**

| How many?      |    | How much?            | P (MW) | Q (MVAR)         |
|----------------|----|----------------------|--------|------------------|
|                | -  |                      |        |                  |
| Buses          | 6  | Total Gen Capacity   | 1110.0 | -900.0 to +900.0 |
| Generators     | 3  | On-line Capacity     | 1110.0 | -900.0 to +900.0 |
| Committed Gens | 3  | Generation (current) | 770.0  | 68.3             |
| Loads          | 5  | Load                 | 770.0  | 0.0              |
| Branches       | 15 | Losses $(I^2 * Z)$   | 0.00   | 68.28            |

| Transformers | 0 | Branch Charging (inj) | -   | 0.0 |
|--------------|---|-----------------------|-----|-----|
| Areas        | 1 | Shunt (inj)           | 0.0 | 0.0 |
| Inter-ties   | 0 | Total Inter-tie Flow  | 0.0 | 0.0 |

|  | Minimum                                      | Maximum   |  |  |
|--|--|---|--|--|
| Voltage Magnitude<br>Voltage Angle<br>P Losses (I^2*R)<br>Q Losses (I^2*X) | 0.996 p.u. @ bus 5<br>-2.50 deg @ bus 5<br>- | 1.000 p.u. @ bus 1<br>5.43 deg @ bus 6<br>0.00 MW @ line 1-2<br>16.74 MVAR @ line 2-6 |  |  |
|  |  |   |  |  |

1

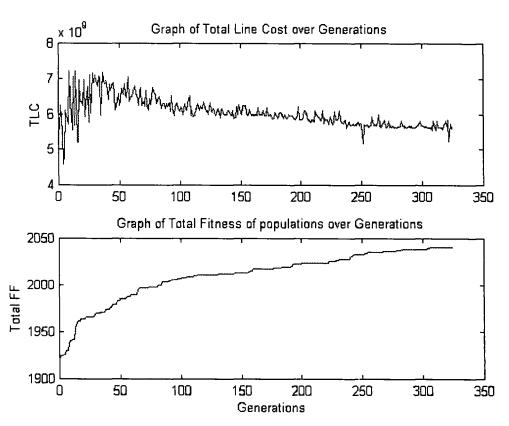
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# **Bus Data**

| Bus Voltage |         | Gen      | eration | Load     |        |          |
|-------------|---------|----------|---------|----------|--------|----------|
| #           | Mag(pu) | Ang(deg) | P (MW)  | Q (MVAR) | P (MW) | Q (MVAR) |
|             |         |          |         |          |        |          |
| 1           | 1.000   | 0.000    | 70.00   | 16.09    | 90.00  | 0.00     |
| 2           | 0.998   | 0.078    | -       | -        | 240.00 | 0.00     |
| 3           | 1.000   | 3.585    | 300.00  | 20.92    | 40.00  | 0.00     |
| 4           | 0.996   | -1.361   | -       | -        | 160.00 | 0.00     |
| 5           | 0.996   | -2.496   | -       | -        | 240.00 | 0.00     |
| 6           | 1.000   | 5.430    | 400.00  | 31.27    | -      | -        |
|             |         |          |         |          |        |          |
|             | Tot     | al:      | 770.00  | 68.28    | 770.00 | 0.00     |

#### **Branch Data**

| From | То  | From B  | us Injection | To Bus I         | njection | Loss (I^ | 2 * Z)   |
|------|-----|---------|--------------|------------------|----------|----------|----------|
| Bus  | Bus | P (MW)  | Q (MVA       | R) P(MW)         | Q (MVAR) | P (MW)   | Q (MVAR) |
|      |     |         |              | www.lifemmrae.lk |          |          |          |
| 1    | 2   | -3.98   | 6.79         | 3.98             | -6.77    | 0.000    | 0.02     |
| 1    | 3   | -31.27  | 0.98         | 31.27            | 0.98     | 0.000    | 1.96     |
| 1    | 4   | 11.83   | 2.15         | -11.83           | -1.86    | 0.000    | 0.29     |
| 1    | 5   | 37.71   | 4.55         | -37.71           | -2.89    | 0.000    | 1.66     |
| 1    | 6   | -34.29  | 1.63         | 34.29            | 1.63     | 0.000    | 3.25     |
| 2    | 3   | -117.37 | -0.86        | 117.37           | 8.06     | 0.000    | 7.20     |
| 2    | 4   | 16.54   | 1.34         | -16.64           | -0.92    | 0.000    | 0.42     |
| 2    | 5   | 35.69   | 2.37         | -35.69           | -0.77    | 0.000    | 1.61     |
| 2    | 6   | -178.96 | 3.91         | 178.96           | 12.83    | 0.000    | 16.74    |
| 3    | 4   | 33.95   | 3.05         | -33.95           | -0.12    | 0.000    | 2.94     |
| 3    | 5   | 91.73   | 8.60         | -91.73           | 1.16     | 0.000    | 9.76     |
| 3    | 6   | -14.31  | 0.23         | 14.31            | 0.23     | 0.000    | 0.46     |
| 4    | 5   | 8.54    | 0.20         | -8.54            | -0.03    | 0.000    | 0.17     |
| 4    | 6   | -106.11 | 2.69         | 106.11           | 9.92     | 0.000    | 12.61    |
| 5    | 6   | -66.33  | 2.53         | 66.33            | 6.67     | 0.000    | 9.20     |
|      |     |         |              |                  | Total:   | 0.000    | 68.28    |



Detailed No 10 result;

From To Line Type

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l

| 1<br>1<br>1<br>1<br>2<br>2<br>2<br>2<br>2<br>3<br>3<br>3 | 2<br>3<br>4<br>5<br>6<br>3<br>4<br>5<br>6<br>4<br>5<br>6<br>5 | Lynx 500 Oil Filled 300 XLPE Lynx Lynx Lynx 300 XLPE 300 XLPE 300 XLPE 300 XLPE 1xGoat Lynx 300 XLPE |
|--|---|--|
|  | -   |  |
| 4  | 6<br>6  | Lynx<br>1 x Zebra  |
| ,  | U   | 1 ALCOIA   |

Total cost (in millions) = 6475 Total number of lines = 15 Total Line length (in km) = 1090

**System Summary** 

| How many?      |    | How much?             | P (MW) | Q (MVAR)         |
|----------------|----|-----------------------|--------|------------------|
|                | -  | **                    |        |                  |
| Buses          | 6  | Total Gen Capacity    | 1110.0 | -900.0 to +900.0 |
| Generators     | 3  | On-line Capacity      | 1110.0 | -900.0 to +900.0 |
| Committed Gens | 3  | Generation (current)  | 770.0  | 86.7             |
| Loads          | 5  | Load                  | 770.0  | 0.0              |
| Branches       | 15 | Losses (I^2 * Z)      | 0.00   | 86.69            |
| Transformers   | 0  | Branch Charging (inj) | -      | 0.0              |
| Areas          | 1  | Shunt (inj)           | 0.0    | 0.0              |
| Inter-ties     | 0  | Total Inter-tie Flow  | 0.0    | 0.0              |

|                   | Minimum            | Maximum              |
|-------------------|--------------------|----------------------|
| Voltage Magnitude | 0.994 p.u. @ bus 4 | 1.000 p.u. @ bus 1   |
| Voltage Angle     | -3.55 deg @ bus 5  | 5.99 deg @ bus 6     |
| P Losses (I^2*R)  | -                  | 0.00 MW @ line 1-2   |
| Q Losses (I^2*X)  | - 1                | 9.41 MVAR @ line 2-6 |

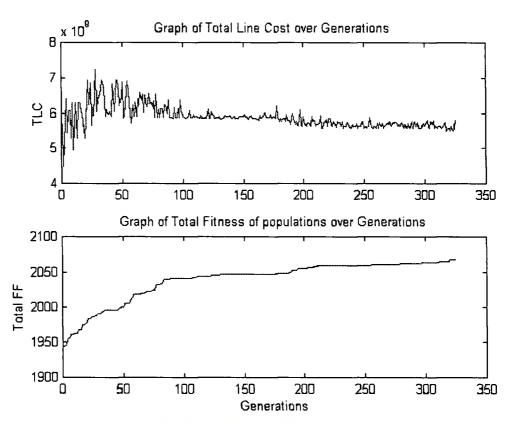
#### **Bus Data**

| Bus Vo  | ltage       | Gener  | ration           | Load   | i        |
|---------|-------------|--------|------------------|--------|----------|
| # Mag(p | u) Ang(deg) | P (MW) | Q (MVAR)         | P (MW) | Q (MVAR) |
|         |             |        |                  |        |          |
| 1 1.000 | 0.000       | 70.00  | 19.68            | 90.00  | 0.00     |
| 2 0.994 | -2.963      | -      | -                | 240.00 | 0.00     |
| 3 1.000 | 2.352       | 300.00 | 25.06            | 40.00  | 0.00     |
| 4 0.994 | -2.349      | in I   | Iniversity of Mo | 160.00 | 0.00     |
| 5 0.994 | -3.548      | (6)    | lectronic These  | 240.00 | 0.00     |
| 6 1.000 | 5.991       | 400.00 | 41.95            | k -    | -        |
|         | Total:      | 770.00 | 86.69            | 770.00 | 0.00     |

#### Branch Data

| From | From To From Bus Injection |         | To Bus   | Injection | Loss (I^2 * Z) |       |          |
|------|----------------------------|---------|----------|-----------|----------------|-------|----------|
| Bus  | Bus                        | P (MW)  | Q (MVAR) |           | Q (MVAR)       | •     | Q (MVAR) |
|      |                            |         |          |           |                |       |          |
| 1    | 2                          | 37.23   | 5.37     | -37.23    | -3.42          | 0.000 | 1.95     |
| 1    | 3                          | -93.27  | 1.91     | 93.27     | 1.91           | 0.000 | 3.83     |
| 1    | 4                          | 20.37   | 3.53     | -20.37    | -2.68          | 0.000 | 0.85     |
| 1    | 5                          | 53.50   | 6.89     | -53.50    | -3.54          | 0.000 | 3.35     |
| 1    | 6                          | -37.81  | 1.98     | 37.81     | 1.98           | 0.000 | 3.96     |
| 2    | 3                          | -80.06  | -1.54    | 80.06     | 9.01           | 0.000 | 7.46     |
| 2    | 4                          | -7.05   | 0.13     | 7.05      | -0.05          | 0.000 | 0.08     |
| 2    | 5                          | 8.08    | -0.01    | -8.08     | 0.10           | 0.000 | 0.08     |
| 2    | 6                          | -123.75 | 4.85     | 123.75    | 14.56          | 0.000 | 19.41    |
| 3    | 4                          | 29.62   | 3.48     | -29.62    | -1.03          | 0.000 | 2.45     |
| 3    | 5                          | 87.71   | 9.68     | -87.71    | -0.61          | 0.000 | 9.07     |
| 3    | 6                          | -30.66  | 0.97     | 30.66     | 0.97           | 0.000 | 1.95     |
| 4    | 5                          | 8.27    | 0.00     | -8.27     | 0.17           | 0.000 | 0.17     |
| 4    | 6                          | -125.34 | 3.76     | 125.34    | 14.55          | 0.000 | 18.31    |
| 5    | 6                          | -82.44  | 3.89     | 82.44     | 9.89           | 0.000 | 13.78    |
|      |                            |         |          |           |                |       |          |

Total: 0.000 86.69



When this program run for different population sizes and different number of generations the result given by the program has some problems like increasing the number of over loaded line, under loaded lines and decrease the line fitness of the final results. By analyzing the following results that can be verified.

Detailed No 11 result; Population size=40 and Number of generations=325

| To | Line Type                                 |
|----|---|
| 2  | 300 XLPE                                  |
| 3  | 300 XLPE                                  |
| 5  | 1xZebra                                   |
| 3  | Lynx                                      |
| 4  | Lynx                                      |
| 5  | 1xGoat                                    |
| 5  | Lynx                                      |
| 6  | 300 XLPE                                  |
| 5  | 300 XLPE                                  |
| 6  | Bear                                      |
|    | 2<br>3<br>5<br>3<br>4<br>5<br>5<br>6<br>5 |

Total cost (in millions) = 3970 Total number of lines = 10 Total Line length (in km) = 640 Newton's method power flow converged in 4 iterations.

| System Sum   | mary         |                                      |          |                  |
|--|--------------|--------------------------------------|----------|------------------|
| Converged in 0   | .01 se       | conds                                |          | <del></del>      |
| How many?  |              | How much?                            | P (MW)   | Q (MVAR)         |
| Buses  | - <b>-</b> 6 | Total Gen Capacity                   | 1110.0   | -900.0 to +900.0 |
| Generators   | 3            | On-line Capacity                     | 1110.0   | -900.0 to +900.0 |
| Committed Gen  | s 3          | Generation (current)                 | 770.0    | 207.2            |
| Loads  | 5            | Load                                 | 770.0    | 0.0              |
| Branches   | 10           | Losses $(I^2 * Z)$                   | 0.00     | 207.21           |
| Transformers   | 0            | Branch Charging (inj)                | -        | 0.0              |
| Areas  | 1            | Shunt (inj)                          | 0.0      | 0.0              |
| Inter-ties   | 0            | Total Inter-tie Flow                 | 0.0      | 0.0              |
|  |              | Minimum                              | Maxim    | um               |
| Voltage Magni<br>Voltage Angle<br>P Losses (I^2*)<br>Q Losses (I^2*) | R)           | 0.963 p.u. @ bus 4 -2.12 deg @ bus 5 | 23.38 de | g @ bus 6        |

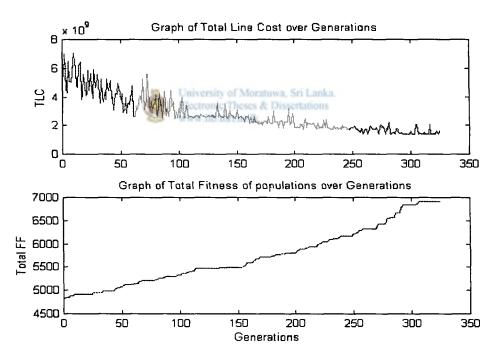
| Bu  | s Data  | ·        | <br>=======   |          |        |          |  |  |
|-----|---------|----------|---------------|----------|--------|----------|--|--|
| Bus | Vol     | ltage    | ge Generation |          |        | Load     |  |  |
| #   | Mag(pu) | Ang(deg) | P (MW)        | Q (MVAR) | P (MW) | Q (MVAR) |  |  |
|     |         |          |               |          |        |          |  |  |
| 1   | 1.000   | 0.000    | 70.00         | 33.21    | 90.00  | 0.00     |  |  |
| 2   | 0.981   | -1.702   | -             | -        | 240.00 | 0.00     |  |  |
| 3   | 1.000   | 8.310    | 300.00        | 78.04    | 40.00  | 0.00     |  |  |
| 4   | 0.963   | 4.867    | -             | -        | 160.00 | 0.00     |  |  |
| 5   | 0.984   | -2.123   | -             | -        | 240.00 | 0.00     |  |  |
| 6   | 1.000   | 23.379   | 400.00        | 95.96    | -      | -        |  |  |
|     |         |          |               |          |        |          |  |  |
|     | Total:  |          | 770.00        | 207.21   | 770.00 | 0.00     |  |  |

| B1   | ranch 1 | Data<br>           |          |         |           |                |          |  |
|------|---------|--------------------|----------|---------|-----------|----------------|----------|--|
| From | то То   | From Bus Injection |          |         | Injection | Loss (I^2 * Z) |          |  |
| Bus  | Bus     | P (MW)             | Q (MVAR) | P (MW)  | Q (MVAR)  | P (MW)         | Q (MVAR) |  |
|      |         |                    |          |         |           |                |          |  |
| 1    | 2       | 19.43              | 12.83    | -19.43  | -12.02    | 0.000          | 0.81     |  |
| 1    | 3       | -72.27             | 5.25     | 72.27   | 5.25      | 0.000          | 10.50    |  |
| 1    | 5       | 32.84              | 15.12    | -32.84  | -13.67    | 0.000          | 1.45     |  |
| 2    | 3       | -148.34            | -3.06    | 148.34  | 29.36     | 0.000          | 26.30    |  |
| 2    | 4       | -78.33             | 17.34    | 78.33   | -8.12     | 0.000          | 9.23     |  |
| 2    | 5       | 6.09               | -2.26    | -6.09   | 2.31      | 0.000          | 0.05     |  |
| 3    | 5       | 154.94             | 28.15    | -154.94 | 0.36      | 0.000          | 28.52    |  |
| 3    | 6       | -115.54            | 15.28    | 115.54  | 15.28     | 0.000          | 30.56    |  |
| 4    | 5       | 46.13              | -5.19    | -46.13  | 11.00     | 0.000          | 5.81     |  |
| 4    | 6       | -284.46            | 13.31    | 284.46  | 80.67     | 0.000          | 93.98    |  |
|      |         |                    |          |         |           |                |          |  |

Total:

0.000

207.21



Detailed No 12 result; Population size=20 and Number of generations=1000

| From | То | Line Type |
|------|----|-----------|
| 1    | 5  | Lynx      |
| 2    | 3  | Lynx      |
| 3    | 5  | 300 XLPE  |
| 4    | 6  | 300 XLPE  |

# 5 6 Lynx

Total cost (in millions) = 1600 Total number of lines = 5 Total Line length (in km) = 290

Newton's method power flow converged in 4 iterations.

|  | ===  |   |                |   |  |
|--|------|---|----------------|---|--|
| System Summ  | nary |   |                |   |  |
| Converged in 0.0   | 0 se | conds                                   |                |   |  |
| How many?  |      | How much?                               | P (MW)         | Q (MVAR)  |  |
| Buses  | 6    | Total Gen Capacity                      | 1110.0         | -900.0 to +900.0  |  |
| Generators   | 3    | On-line Capacity                        | 1110.0         | -900.0 to +900.0  |  |
| Committed Gens   | 3    | Generation (current)                    | 770.0          | 241.4   |  |
| Loads  | 5    | Load                                    | 770.0          | 0.0   |  |
| Branches   | 5    | Losses $(I^2 * Z)$                      | 0.00           | 241.42  |  |
| Transformers   | 0    | Branch Charging (inj)                   | -              | 0.0   |  |
| Areas  | 1    | Shunt (inj)                             | 0.0            | 0.0   |  |
| Inter-ties   | 0    | Total Inter-tie Flow                    | 0.0            | 0.0   |  |
| University of Moratuwa, Sri Lanka. Elect Minimum Dissertations Maximum     |      |   |                |   |  |
| Voltage Magnitude<br>Voltage Angle<br>P Losses (I^2*R)<br>Q Losses (I^2*X) |      | 0.958 p.u. @ bu<br>-13.91 deg @ bu<br>- | s 2 32<br>0.00 | 000 p.u. @ bus 1<br>.24 deg @ bus 6<br>MW @ line 1-5<br>7 MVAR @ line 5-6 |  |

| Bus | Vol     | tage       | Generation |          | Lo     | ad       |                                       |
|-----|---------|------------|------------|----------|--------|----------|---------------------------------------|
| #   | Mag(pu  | ) Ang(deg) | P (MW)     | Q (MVAR) | P (MW) | Q (MVAR) |                                       |
| 1   | 1.000   | 0.000      | 70.00      | 28.11    | 90.00  | 0.00     |                                       |
| 2   | 0.958   | -13.911    | -          | -        | 240.00 | 0.00     | Charles .                             |
| 3   | 1.000   | 2.842      | 300.00     | 98.14    | 40.00  | 0.00     | · · · · · · · · · · · · · · · · · · · |
| 4   | 0.979   | 20.453     | -          | -        | 160.00 | 0.00     | ,                                     |
| 5   | 0.968   | 1.362      | -          | -        | 240.00 | 0.00     |                                       |
| 6   | 1.000   | 32.242     | 400.00     | 115.17   | -      | -        | × ;                                   |
|     | <b></b> |            |            |          |        |          |                                       |
|     | Tota    | l:         | 770.00     | 241.42   | 770.00 | 0.00     |                                       |

| Bra   | anch I                | Data   |   |   |   |   |  |
|---|-----------------------|--|---|---|---|---|--|
| From To Bus Bus   |                       | From Bus Injection P (MW) Q (MVAR)               |   | To Bus Injection P (MW) Q (MVAR)              |   | Loss (I^2 * Z)<br>P (MW) Q (MVAR)         |  |
| 1<br>2<br>3<br>4<br>5   | 5<br>3<br>5<br>6<br>6 | -20.00<br>-240.00<br>20.00<br>-160.00<br>-240.00 | 28.11<br>0.00<br>25.90<br>0.00<br>51.30 | 20.00<br>240.00<br>-20.00<br>160.00<br>240.00 | -26.74<br>72.24<br>-24.56<br>33.39<br>81.77 | 0.000<br>0.000<br>0.000<br>0.000<br>0.000 | 1.37<br>72.24<br>1.34<br>33.39<br>133.07 |
|   | 8 r                   | ( 10 <sup>9</sup>                                | Total:<br>Graph of To                   | tal Line Cost                                 | over Generatio                              | 0.000                                     | 241.42                                   |
|   | 2 - 2 -               |  |   |   |   |   |  |
| O 100 200 300 400 500 600 700 800 900  Graph of Total Fitness of populations over Generations |                       |  |   |   |   |   | 00 1000<br>                              |
| t i   | 2600                  | -  |   |   | .r  | سممم                                      | 1  |
| Total FF  | 2400<br>2200<br>2000  |  |   |   |   |   |  |
|   | 1800 <sup>(</sup>     | 100  | 200 300                                 | 400 500<br>Generati                           | 600 700<br>ons                              | 800 9                                     | J<br>00 1000                             |

# 6.2 Conclusion

The research reported in this thesis clearly demonstrates that a GA approach to a Transmission Network Planning problem is both feasible and advantageous. It provides to optimize several parameters in the same time.

Furthermore, it allows the representation of non-linearities which are hard to include in pure mathematical programming methods; in fact, the existence of non-linearities

enhances the advantages of using GA against pure mathematical programming. These non-linearities arise not only from the non-linear character of objective functions and constraints but also from the discrete nature of many aspects of the distribution planning problem. These in some cases could lead to a non-convex domain, but GA are able to deal with such environments and can detect local minima or even "islands" of solutions.

The result of a GA are a generation of solutions filtered through the struggle for survival. Therefore, many interesting and valuable exercises on comparisons and trade offs may be executed, helping the planner to gain insight on the problem he is faced with and allowing field for better decisions to be taken.

Since GA program starts with randomly generated solutions and ad all other operations randomly, we can obtained several different results for the same problem. So can select the best among them.





# **MATPOWER**

# A MATLAB™ Power System Simulation Package

Version 2.0
December 24, 1997



# **User's Manual**

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© 1997 Power Systems Engineering Research Center (PSERC) School of Electrical Engineering, Cornell University, Ithaca, NY 14853

# 1 Introduction

#### What is MATPOWER?

MATPOWER is a package of Matlab m-files for solving power flow and optimal power flow problems. It is intended as a simulation tool for researchers and educators which will be easy to use and modify. MATPOWER is designed to give the best performance possible while keeping the code simple to understand and modify. The MATPOWER home page can be found at:

http://www.pserc.cornell.edu/matpower/matpower.html

#### Where did it come from?

MATPOWER was developed by Ray Zimmerman and Deqiang Gan of PSERC at Cornell University (http://www.pserc.cornell.edu/) under the direction of Robert Thomas. The initial need for Matlab based power flow and optimal power flow code was born out of the computational requirements of the PowerWeb project (see http://www.pserc.cornell.edu/powerweb/).

#### Who can use it?

MATPOWER is free. Anyone may use it. Anyone may modify it for their own use as long as the original copyright notices remain in place. Please don't distribute modified versions of MATPOWER without written permission from us.

# 2 Getting Started

# 2.1 System Requirements

To use MATPOWER you will need a Mac, UNIX machine, or PC with:

- Matlab 4 or higher (available from The MathWorks)
- Matlab Optimization Toolbox (available from The MathWorks1)

#### 2.2 Installation

Step 1: Go to the MATPOWER home page2 and follow the download instructions.

Step 2: Unpack the archive using the appropriate software for your machine (StuffIt Expander for Mac, gunzip and tar for UNIX, pkzip, WinZip, etc. for PC).

Step 3: Copy all of the m-files in the MATPOWER distribution to a location in your Matlab path.

<sup>1</sup> See http://www.mathworks.com/

<sup>2</sup> http://www.pserc.comell.edu/matpower/matpower.html

# 2.3 Running a Power Flow

To run a simple Newton power flow on the default 9-bus system specified in the file case.m, with the default algorithm options, at the Matlab prompt, type:

```
>> runpf
```

To run a power flow on the 118-bus system whose data is in case118.m, type:

```
>> runpf('case118')
```

# 2.4 Running an Optimal Power Flow

To run an optimal power flow on the default 9-bus system specified in the file case.m, with the default algorithm options, at the Matlab prompt, type:

```
>> runopf
```

To run an optimal power flow on the 30-bus system whose data is in case 30.m, type:

```
>> runopf('case30')
```

To run an optimal power flow on the same system, but with the option for MATPOWER to shut down (decommit) expensive generators, type:

```
>> runuopf('case30')
```

# 2.5 Getting Help

As with Matlab's built-in functions and toolbox routines, you can type help followed by the name of a command or m-file to get help on that particular function. Nearly all of *MATPOWER*'s m-files have such documentation. For example, the help for runopf looks like:

```
>>> help runopf
RUNOPF Runs an optimal power flow.
[baseMVA, bus, gen, gencost, branch, f, success, et] = ...
runopf(casename, mpopt, fname)
```

www.lib.mrt.ac.lk

Runs an optimal power flow where casename is the name of the m-file (without the .m extension) containing the opf data, and mpopt is a MATPOWER options vector (see 'help mpoption' for details). Uses default options if 2nd parameter is not given, and 'case' if 1st parameter is not given. The results may optionally be printed to a file (appended if the file exists) whose name is given in fname (in addition to printing to STDOUT). Optionally returns the final values of baseMVA, bus, gen, gencost, branch, f, success, and et.

MATPOWER also has many options which control the algorithms and the output. Type:

>> help mpoption

and see Section 3.5 for more information on MATPOWER's options.

# 3 Technical Reference

#### 3.1 Data File Format

The data files used by MATPOWER are simply Matlab m-files which define and return the variables baseMVA, bus, branch, gen, area, and gencost. The bus, branch, and gen variables are matrices. Each row in the matrix corresponds to a single bus, branch, or generator, respectively. The columns are similar to the columns in the standard IEEE and PTI formats. The details of the specification of the MATPOWER case file can be found in the help for case.m:

#### >> help case

CASE Defines the power flow data in a format similar to PTI. [baseMVA, bus, gen, branch, area, gencost] = case
The format for the data is similar to PTI format except where noted.
An item marked with (+) indicates that it is included in this data but is not part of the PTI format. An item marked with (-) is one that is in the PTI format but is not included here.

```
Bus Data Format
```

```
1 bus number (1 to 29997) Moraluwa Sri Lanka
      2 bus type
                        Electronic Theses & Dissertations
            PQ bus = 1
                        www.lib.mrt.ac.lk
            PV bus = 2
            reference bus = 3
            isolated bus = 4
      3 Pd, real power demand (MW)
      4 Qd, reactive power demand (MVAR)
      5 Gs, shunt conductance (MW (demanded?) at V = 1.0 p.u.)
      6 Bs, shunt susceptance (MVAR (injected?) at V = 1.0 p.u.)
      7 area number, 1-100
      8 Vm, voltage magnitude (p.u.)
      9 Va, voltage angle (degrees)
(-)
      (bus name)
      10 baseKV, base voltage (kV)
      11 zone, loss zone (1-999)
(+)
      12 maxVm, maximum voltage magnitude (p.u.)
      13 minVm, minimum voltage magnitude (p.u.)
Generator Data Format
      1 bus number
      (machine identifier, 0-9, A-Z)
      2 Pg, real power output (MW)
      3 Qg, reactive power output (MVAR)
      4 Qmax, maximum reactive power output (MVAR)
      5 Qmin, minimum reactive power output (MVAR)
      6 Vg, voltage magnitude setpoint (p.u.)
(-)
       (remote controlled bus index)
```

```
7 mBase, total MVA base of this machine, defaults to baseMVA
      (machine impedance, p.u. on mBase)
(-)
      (step up transformer impedance, p.u. on mBase)
(-)
(-)
      (step up transformer off nominal turns ratio)
      8 status, 1 - machine in service, 0 - machine out of service
      (% of total VARS to come from this gen in order to hold V at
      remote bus controlled by several generators)
      9 Pmax, maximum real power output (MW)
      10 Pmin, minimum real power output (MW)
Branch Data Format
      1 f, from bus number
      2 t, to bus number
(-)
       (circuit identifier)
      3 r, resistance (p.u.)
      4 x, reactance (p.u.)
      5 b, total line charging susceptance (p.u.)
      6 rateA, MVA rating A (long term rating)
      7 rateB, MVA rating B (short term rating)
      8 rateC, MVA rating C (emergency rating)
      9 ratio, transformer off nominal turns ratio ( = 0 for lines )
      (taps at 'from' bus, impedance at 'to' bus, i.e. ratio = Vf / Vt)
      10 angle, transformer phase shift angle (degrees)
(-)
       (Gf, shunt conductance at from bus p.u.)
(-)
       (Bf, shunt susceptance at from bus p.u.)
(-)
       (Gt, shunt conductance at to bus p.u.)
(-)
      (Bt, shunt susceptance at to bus p.u.)
      11 initial branch status, 1 in service, 0 - out of service
                        Electronic Theses & Dissertations
                        www.lib.mrt.ac.lk
(+) Area Data Format
      1 i, area number
      2 price_ref_bus, reference bus for that area
(+) Generator Cost Data Format
      NOTE: If gen has n rows, then the first n rows of gencost contain
      the cost for active power produced by the corresponding
      generators. If gencost has 2*n rows then rows n+1 to 2*n contain
      the reactive power costs in the same format.
      1
            model, 1 - piecewise linear, 2 - polynomial
      2
            startup, startup cost in US dollars
      3
            shutdown, shutdown cost in US dollars
            n, number of cost coefficients to follow for polynomial
            (or data points for piecewise linear) total cost function
            and following, cost data, piecewise linear data as:
            x0, y0, x1, y1, x2, y2, ...
            and polynomial data as, e.g.:
            c2, c1, c0
            where the polynomial is c0 + c1*P + c2*P^2
```

#### 3.2 Power Flow

MATPOWER has three power flow solvers. The default power flow solver is based on a standard Newton's method [11] using a full Jacobian, updated at each iteration. This method is described in detail in many textbooks. The other two power flow solvers are

variations of the fast-decoupled method [9]. MATPOWER implements the XB and BX variations as described in [1]. Currently, MATPOWER's power flow solvers do not include any transformer tap changing or feasibility checking capabilities.

Performance of the power flow solvers should be excellent even on very large-scale power systems, since the algorithms and implementation take advantage of Matlab's built-in sparse matrix handling. On a Sun Ultra 2200, MATPOWER solves a 9600-bus test case in about 10 seconds, and a 38400 bus case in about 50 seconds.

# 3.3 Optimal Power Flow

MATPOWER includes two solvers for the optimal power flow (OPF) problem. The first is based on the constr function included in Matlab's Optimization Toolbox, which uses a successive quadratic programming technique with a quasi-Newton approximation for the Hessian matrix. The second approach is based on linear programming. It can use the LP solver in the Optimization Toolbox or other Matlab LP solvers available from third parties.

The performance of MATPOWER's OPF solvers depends on several factors. First, the constr function uses an algorithm which does not exploit or preserve sparsity, so it is inherently limited to small power systems. The LP-based algorithm, on the other hand, does preserve sparsity. However, the LP-solver included in the Optimization Toolbox does not exploit this sparsity. In fact, the LP-based method with the default LP solver performs worse than the constr-based method, even on small systems. Fortunately, there are LP-solvers available from third parties which do exploit sparsity. In general, these yield much higher performance. One in particular, called bpmpd [7] (actually a QP-solver), has proven to be robust and efficient.

It should be noted, however, that even with a good LP-solver, *MATPOWER*'s LP-based OPF solver, unlike it's power flow solver, is not suitable for very-large scale problems. Substantial improvements in performance may still be possible, though they may require significantly more complicated coding and possibly a custom LP-solver. On a Sun Ultra 2200, the LP-based OPF solver using *bpmpd* solves a 30-bus system in under 4 seconds and a 118-bus case in under 25 seconds.

#### **OPF** Formulation

The OPF problem solved by MATPOWER is a "smooth" OPF with no discrete variables or controls. The objective function is the total cost of real and/or reactive generation. These costs may be defined as polynomials or as piecewise-linear functions of generator output. The problem is formulated as follows:

min
$$P_{g,Q_g} \sum f_{1i}(P_{gi}) + f_{2i}(Q_{gi})$$
such that ...
$$P_{gi} - P_{Li} - P(V,\theta) = 0 \quad \text{(active power balance equations)}$$

```
Q_{gi}-Q_{Li}-Q(V,\theta)=0 (reactive power balance equations)

S_{ij}^f \leq S_{ij}^{max} (apparent power flow limit of lines, from side)

S_{ij}^t \leq S_{ij}^{max} (apparent power flow limit of lines, to side)

V_i^{min} \leq V_i \leq V_i^{max} (bus voltage limits)

P_{gi}^{min} \leq P_{gi} \leq P_{gi}^{max} (active power generation limits)

Q_{gi}^{min} \leq Q_{gi} \leq Q_{gi}^{max} (reactive power generation limits)
```

Here  $f_{ii}$  and  $f_{2i}$  are the costs of active and reactive power generation, respectively, for generator I at a given dispatch point. Both  $f_{1i}$  and  $f_{2i}$  are assumed to be a polynomial or piecewise-linear functions. The problem can be written more compactly in the following form:

```
\min_{x} f(x_2)
such that ...
g(x) \le 0
```

where f and g are non-linear functions.

### Optimization Toolbox Based OPF Solver (constr)

The first of the two OPF solvers in MATPOWER is based on the constr non-linear constrained optimization function in Matlab's Optimization Toolbox. The constr function and the algorithms it uses are covered in the Optimization Toolbox manual [5]. MATPOWER provides constr with two m-files which it uses during for the optimization. One computes the objective function, f, and the constraint violations, g, at a given point, x, and the other computes their gradients  $\partial f/\partial x$  and  $\partial g/\partial x$ .

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MATPOWER has two versions of these m-files. One set is used to solve systems with polynomial cost functions. In this formulation, the cost functions are included in a straightforward way into the objective function. The other set is used to solve systems with piecewise-linear costs. Piecewise-linear cost functions are handled by introducing a cost variable for each piecewise-linear cost function. The objective function is simply the sum of these cost variables which are then constrained to lie above each of the linear functions which make up the piecewise-linear cost function. Clearly, this method works only for convex cost functions. In the MATPOWER documentation this will be referred to as a constrained cost variable (CCV) formulation.

The algorithm codes 100 and 200, respectively, are used to identify the conser-based solver for polynomial and piecewise-linear cost functions. If algorithm 200 is chosen for a system with polynomial cost function, the cost function will be approximated by a piecewise-linear function by evaluating the polynomial at a fixed number of points determined by the options vector (see Section 3.5 for more details on the MATPOWER

options). It should be noted that the constr-based method can also benefit from a superior QP-solver such as *bpmpd*. See Appendix A for more information on LP and QP-solvers.

#### LP-Based OPF Solver (LPconstr)

Linear programming based OPF methods are in wide use today in the industry. However, the LPbased algorithm included in *MATPOWER* is much simpler than the algorithms used in productiongrade software.

The LP-based methods in MATPOWER use the same problem formulation as the constrbased methods, including the CCV formulation for the case of piecewise-linear costs. The compact form of the OPF problem can be rewritten to partition g into equality and inequality constraints, and to partition the variable x as follows:

```
\min_{x} f(x_2)
such that ...
g_1(x_1, x_2) = 0 \text{ (equality constraints)}
g_2(x_1, x_2) \le 0 \text{ (inequality constraints)}
```

where  $x_1$  contains the system voltage magnitudes and angles, and  $x_2$  contains the generator real and reactive power outputs (and corresponding cost variables for the CCV formulation). This is a general non-linear programming problem, with the additional assumption that the equality constraints can be used to solve for  $x_1$ , given a value for  $x_2$ . The LP-based OPF solver is implemented with a function LPconstr, which is similar to constr in that it uses the same m-files for computing the objective function, constraints, and their respective gradients. In addition, a third m-file (lpeqslvr.m) is needed to solve for  $x_1$  from the equality constraints, given a value for  $x_2$ . This architecture makes it relatively simple to modify the formulation of the problem and still be able to use both the constr-based and LP-based solvers.

The algorithm proceeds as follows, where the superscripts denote iteration number:

Step 0: Set iteration counter  $k \leftarrow 0$  and choose an appropriate initial value, call it  $x_{20}$ , for  $x_2$ .

Step 1: Solve the equality constraint (power flow) equations  $g_1(x_{1k}, x_{2k}) = 0$  for  $x_{1k}$ .

Step 2: Linearize the problem around  $x_k$ , solve the resulting LP for  $\Delta x$ .

$$\min_{\Delta x} \left[ \frac{\partial f}{\partial x} \Big|_{x=x^4} \right] . \Delta x$$

such that ...

$$\min_{\Delta x} \left[ \frac{\partial f}{\partial x} \Big|_{x=x^{4}} \right] \Delta x \le -g(x^{k})$$
$$-\Delta \le \Delta x \le \Delta$$

Step 3: Set  $k \leftarrow k+1$ , update current solution  $x_k = x_{k-1} + \Delta x$ .

Step 4: If xk meets termination criteria, stop, otherwise go to step 5.

Step 5: Adjust step size limit  $\Delta$  based on the trust region algorithm in [3], go to step 1. The termination criteria is outlined below:

$$\frac{\partial L}{\partial x} = \frac{\partial f}{\partial x} + \lambda^{T} \cdot \frac{\partial g}{\partial x} \le \text{tolerance}_{1}$$

 $g(x) \le \text{tolerance}_2$ 

 $\Delta x \le \text{tolerance}_3$ 

Here  $\lambda$  is the vector of Lagrange multipliers of the LP problem. The first condition pertains to the size of the gradient, the second to the violation of constraints, and the third to the step size. More detail can be found in [4].

Quite frequently, the value of xk given by step 1 is infeasible and could result in an infeasible LP problem. In such cases, a slack variable is added for each violated constraint. These slack variables must be zero at the optimal solution.

The LPconstr function implements the following three methods:

- sparse formulation with full set of inequality constraints
- sparse formulation with relaxed constraints (ICS, Iterative Constraint Search)
- dense formulation with relaxed constraints (ICS) [10]

These three methods are specified using algorithm codes 160, 140, and 120, respectively, for systems with polynomial costs, and 260, 240, and 220, respectively, for systems with piecewise-linear costs. As with the *constr*-based method, selecting one of the 2xx algorithms for a system with polynomial cost will cause the cost to be replaced by a piecewise-linear approximation.

In the dense formulation, some of the variables  $x_1$  and the equality constraints  $g_1$  are eliminated from the problem before posing the LP sub-problem. This procedure is outlined below. Suppose the LP sub-problem is given by:  $\min c^T \cdot \Delta x$ 

such that ...

$$A \cdot \Delta x \le b$$
$$-\Delta \le \Delta x \le \Delta$$

If this is rewritten as:  $\min c_1^T \cdot \Delta x_1 + c_2^T \cdot \Delta x_2$ such that ...

$$A_{11}.\Delta x_1 + A_{12}.\Delta x_2 = b_1$$
  

$$A_{21}.\Delta x_1 + A_{22}.\Delta x_2 = b_2$$

 $-\Delta \le \Delta x \le \Delta$ 

Where  $A_{11}$  is a square matrix,  $\Delta x_1$  can be computed as:

$$\Delta x_1 = A_{11}^{-1} (b_1 - A_{12}.\Delta x_2)$$

Substituting back in to the problem, yields a new LP problem:

$$\min(-c_1^T A_{11}^{-1} A_{12} + c_2^T).\Delta x_2$$

such that ...

$$A_{11}.\Delta x_1 + A_{12}.\Delta x_2 = b_1$$

$$A_{21}.A_{11}^{-1}(b_1 - A_{12}\Delta x_2) + A_{22}.\Delta x_2 \le b_1$$

$$-\Delta_1 \le A_{11}^{-1}(b - A_{12}\Delta x_2) \le \Delta_2$$

$$-\Delta_2 \le \Delta x_2 \le \Delta_2$$

This new LP problem is smaller than the original, but it is no longer sparse. As mentioned above, to realize the full potential of the LP-based OPF solvers, it will be necessary to obtain a good LP-solver, such as *bpmpd*. See Appendix A for more details.

# 3.4 Unit Decommitment Algorithm

The standard OPF formulation described in the previous section has no mechanism for completely shutting down generators which are very expensive to operate. Instead they are simply dispatched at their minimum generation limits. *MATPOWER* includes a unit decommitment algorithm which allows it to shut down these expensive units. The algorithm is based on a simplified version of the decommitment technique proposed in [6].

The algorithm proceeds as follows:

Step 0: Assume all generators are on-line with all generator limits in place.

Step 1: Solve a normal OPF.

Step 2: If the OPF converged to a feasible solution and the objective function decreased from the previous iteration (or if this is the first iteration), go to step 3, otherwise go to step 4.

Step 3: Compute a decommitment index for each generator i as follows:

$$d_i = f_i(P_i) - \lambda_i \cdot P_i$$

where  $P_i$  is generator i's dispatch computed by the OPF,  $f_i$  is the cost of operating at  $P_i$ , and  $\lambda_i$  is the Lagrange multiplier on the real power equality constraint at the bus where generator i is located. Continue with step 5.

Step 4: Return to the previous commitment and set d\* to zero (to eliminate it from consideration).

Step 5: Find the generator k with the smallest decommitment index. If  $d_k$  is negative, shut

Down generator k and return to step 1. If  $d_k$  is positive, stop.

### 3.5 MATPOWER Options

MATPOWER uses an options vector to control the many options available. It is similar to the options vector produced by the foptions function in Matlab's Optimization Toolbox. The primary difference is that modifications can be made by option name, as opposed to having to remember the index of each option. The default MATPOWER options vector is obtained by calling mpoption with no arguments. So, typing:

```
>> runopf('case30', mpoption)
```

is another way to run the OPF solver with the all of the default options.

The MATPOWER options vector controls the following:

- power flow algorithm
- power flow termination criterion
- OPF algorithm
- OPF default algorithms for different cost models
- OPF cost conversion parameters
- OPF termination criterion www.lib.mrt.ac.lk
- verbose level
- printing of results

The details are given below:

```
>> help mpoption
```

MPOPTION Used to set and retrieve a MATPOWER options vector.

```
opt = mpoption
```

returns the default options vector

opt = mpoption(name1, value1, name2, value2, ...)
 returns the default options vector with new values for up to 7
 options, name# is the name of an option, and value# is the new
 value. Example: options = mpoption('PF\_ALG', 2, 'PF\_TOL', 1e-4)

opt = mpoption(opt, name1, value1, name2, value2, ...)
 same as above except it uses the options vector opt as a base
 instead of the default options vector.
 The currently defined options are as follows:

idx - NAME, default description [options]

```
power flow options
1 - PF ALG, 1
                               power flow algorithm
      [ 1 - Newton's method
                                                                   ]
        2 - Fast-Decoupled (XB version)
      [ 3 - Fast-Decoupled (BX version)
2 - PF_TOL, 1e-8
                               termination tolerance on per unit
                               P & Q mismatch
                         maximum number of iterations for
3 - PF_MAX_IT, 10
                               Newton's method
4 - PF MAX IT FD, 30
                               maximum number of iterations for
                               fast decoupled method
OPF options
11 - OPF ALG, 0
                               algorithm to use for OPF
      [ (see README for more info on formulations/algorithms)
      [ The algorithm code = F * 100 + S * 20, where ...
      [ F specifies one of the following OPF formulations
            1 - standard (polynomial cost in obj fcn)
            2 - CCV (constrained cost variables)
            S specifies one of the following solvers
                                                                   ٦
            0 - 'constr' from Optimization Toolbox
                                                                   1
            1 - Dense LP-based method
            2 - Sparse LP-based method w/relaxed constraints]
            3 - Sparse LP-based method w/full constraints
            This yields the following 9 codes:
            0 - choose appropriate default from OPF_ALG_POLY
            or OPF ALG PWL
            100 - standard formulation, constr
                                                                   1
            120 - standard formulation, dense LP
                                                                   ]
            140 - standard formulation, sparse LP (relaxed) ]
            160 - standard formulation, sparse LP (full)
                                                                   ]
            200 - CCV formulation, constr
            220 - CCV formulation, dense LP
                                                                   ]
            240 - CCV formulation, sparse LP (relaxed)
            260 - CCV formulation, sparse LP (full)
                                                                   1
12 - OPF_ALG_POLY, 100
                                default OPF algorithm for use with
                                polynomial cost functions
13 - OPF_ALG_PWL, 200
                                 default OPF algorithm for use with
                                 piece-wise linear cost functions
14 - OPF POLY2PWL PTS, 10
                                 number of evaluation points to use
                                 when converting from polynomial to
                                 piece-wise linear costs
15 - OPF NEQ, 0
                                 number of equality constraints
                                 0 => 2*nb, set by program, not a
                                 user option)
16 - OPF VIOLATION, 5e-6
                                 constraint violation tolerance
17 - CONSTR TOL X, 1e-4
                           termination tol on x for 'constr'
18 - CONSTR_TOL_F, 1e-4
                           termination tol on F for 'constr'
19 - CONSTR_MAX_IT, 0
                                 max number of iterations for 'constr'
                                 [ 0 => 2*nb + 150
                                                                   1
20 - LPC TOL GRAD, 3e-3
                           termination tolerance on gradient
                                 for 'LPconstr'
21 - LPC_TOL_X, 5e-3
                                 termination tolerance on x (min
                                 step size) for 'LPconstr'
22 - LPC MAX IT, 1000
                                 maximum number of iterations for
                                 'LPconstr'
```

```
output options
31 - VERBOSE, 1
                                amount of progress info printed
            0 - print no progress info
                                                                   ]
            1 - print a little progress info
                                                                   ]
            2 - print a lot of progress info
                                                                   ]
            3 - print all progress info
32 - OUT_ALL, -1 controls printing of results
           -1 - individual flags control what prints
                                                             ]
           0 - don't print anything
                                                                   ]
            (overrides individual flags, except OUT_RAW)
            1 - print everything
            (overrides individual flags, except OUT RAW)
33 - OUT_SYS_SUM, 1
                               print system summary [ 0 or 1
                               print area summaries [ 0 or 1
34 - OUT AREA SUM, 0
35 - OUT_BUS, 1
                               print bus detail [ 0 or 1
36 - OUT_BRANCH, 1
                               print branch detail [ 0 or 1
37 - OUT_GEN, 0
                                print generator detail [ 0 or 1
                                (OUT BUS also includes gen info)
38 - OUT ALL LIM, -1
                                control constraint info output
      [ -1 - individual flags control what constraint info prints ]
      [ 0 - no constraint info (overrides individual flags) ]
      [ 1 - binding constraint info (overrides individual flags)
      [ 2 - all constraint info (overrides individual flags)
                                                                    ]
39 - OUT_V_LIM, 1 control output of voltage limit info
      [ 0 - don't print University of Moratuwa, Sri Lanka.
      [ 1 - print binding constraints only
                                                                    ]
      [ 2 - print all constraints
                                                                    1
      [ (same options for OUT_LINE_LIM, OUT_PG_LIM, OUT_QG_LIM)
40 - OUT LINE_LIM, 1
                                control output of line limit info
41 - OUT PG LIM, 1
                                control output of gen P limit info
42 - OUT_QG_LIM, 1
                                control output of gen Q limit info
43 - OUT RAW, 0
                                 print raw data for Perl database
                                 interface code [ 0 or 1 ]
A typical usage of the options vector might be as follows:
Get the default options vector:
```

```
>> opt = mpoption;
```

Use the fast-decoupled method to solve power flow:

```
>> opt = mpoption(opt, 'PF_ALG', 2);
```

Display only system summary and generator info:

```
>> opt = mpoption(opt, 'OUT_BUS', 0, 'OUT_BRANCH', 0, 'OUT_GEN', 1);
Show all progress info:
```

```
>> opt = mpoption(opt, 'VERBOSE', 3);
```

```
Now, run a bunch of power flows using these settings:
>> runpf('case57', opt)
>> runpf('case118', opt)
>> runpf('case300', opt)

3.6 Summary of the Files

Documentation files:
README - basic intro to MATPOWER
CHANGES - modification history of MATPOWER
```

## Input data files:

```
cdf2matp.m - a stand-alone m-file which reads IEEE CDF formatted
              data and outputs data in MATPOWER's case.m format
            - same as case9.m
case.m
case9.m
           - a 3 generator, 9 bus case
case30.m
           - a 6 generator, 30 bus case
case57.m
           - IEEE 57-Bus case
case118.m - IEEE 118-Bus case
case300.m - IEEE 300-Bus case
case9Q.m - case9.m, with costs for reactive generation
case30Q.m - case30.m, with costs for reactive generation
case30pwl.m - case30.m with a piece-wise linear cost function
                        University of Moratuwa, Sri Lanka
                    Electronic Theses & Dissertations
```

Source files used by all algorithms: make the

```
bustypes.m
```

dSbus\_dV.m - computes partial derivatives for Jacobian

manual.pdf - PDF version of the MATPOWER User's Manual (requires Adobe Acrobat Reader)

ext2int.m idx\_brch.m idx\_bus.m idx\_gen.m int2ext.m makeSbus.m

makeYbus.m - builds Ybus matrix
mpoption.m - sets MATPOWER options

printpf.m - prints output

#### Other source files used by PF (Power Flow):

fdpf.m - implements fast decoupled power flow
newtonpf.m - implements Newton's method power flow
pfsoln.m

runpf.m - main program for running a power flow
makeB.m

#### Other source files used by OPF (Optimal Power Flow):

dAbr\_dV.m - computes partial derivatives of apparent power flows
dSbr\_dV.m - computes partial derivatives of complex power flows
fg\_names.m

```
fun ccv.m
            - computes obj fcn and constraints for CCV formulation
fun std.m - computes obj fcn and constraints for standard formulation
grad_ccv.m - computes gradients for standard formulation
grad std.m - computes gradients for standard formulation
idx area.m
idx cost.m
opf.m - implements main OPF routine
opfsoln.m
opf_form.m
opf_slvr.m
poly2pwl.m
pqcost.m
            - main program for running an optimal power flow
runopf.m
totcost.m - computes cost
The following are used only by the LP-based OPF algorithms:
      LPconstr.m
      LPeqslvr.m
      LPrelax.m
      LPsetup.m
Other source files used by UOPF (Unit decommitment/OPF):
(all files from OPF, except runopf.m)
uopf.m - implements decommitment heuristic
runuopf.m - main program for running OPF with decommitment algorithm
                         University of Moratuwa, Sri Lanka.
Files for use with the bpmpd LP/QP-solver:
                        www.lib.mrt.ac.lk
bpmpd/lp.m-replacement for Optimization Toolbox lp.m
bpmpd/qp.m-replacement for Optimization Toolbox qp.m (used by constr.m)
```

# 4 Acknowledgments

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## Genetic Algorithms: Diophantine Equation Solver

This is a C++ program that solves a diophantine equation using genetic algorithms

#### **CDiophantine**

Firstly the class header (note for formatting reasons, a lot of the documentation is taken out):

```
#include <stdlib.h>
#include <time.h>
#define MAXPOP 25
struct gene {
   int alleles[4];
   int fitness;
   float likelihood;
   // Test for equality.
   operator == (gene gn) {
       for (int i=0;i<4;i++) {
          if (gn.alleles[i] != alleles[i]) return false;
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                             Electronic Theses & Dissertations
                             www.lib.mrt.ac.lk
      return true;
   }
};
class CDiophantine {
   public:
       CDiophantine(int, int, int, int, int);
       int Solve();
       // Returns a given gene.
       gene GetGene(int i) { return population[i];}
   protected:
       int ca, cb, cc, cd;
       int result:
       gene population[MAXPOP];
       int Fitness(gene &);
       void GenerateLikelihoods();
       float MultInv();inverse.
       int CreateFitnesses();
```

```
void CreateNewPopulation();
    int GetIndex(float val);

gene Breed(int pl, int p2);
};
```

Firstly you notice that there are two structures, the gene structure and the actual CDiophantine class. The gene structure is used to keep track of the different solution sets. The population generated is a population of genes. The gene structure keeps track of its own fitness and likelihood values itself

#### **Fitness function**

The fitness functions calculate the fitness of each gene. In our case the fitness function is the difference between the calculated value of the gene and the result we want. This class uses two functions, one that calculates all the fitnesses and another smaller one (you should probably make the function inline) to calculate it per gene.

```
int CDiophantine::Fitness(gene &gn) {
   int total = ca * gn.alleles[0] + cb * gn.alleles[1]
              + cc * gn.alleles[2] + cd * gn.alleles[3];
   return gn.fitness = abs(total - result);
}
                            Electronic Theses & Dissertations
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int CDiophantine::CreateFitnesses() {
   float avgfit = 0;
   int fitness = 0;
   for(int i=0;i<MAXPOP;i++) {</pre>
      fitness = Fitness(population[i]);
      avgfit += fitness;
      if (fitness == 0) {
         return i;
   }
   return 0;
}
```

Note that if the fitness is zero, then a solution has been found - so return the index. After we calculate the fitnesses, we then have to calculate the likelihoods of the gene's being chosen.

#### Likelihood functions

We calculate the likelihood by first calculating the sum of the multiplicative inverses, then by dividing the inverse of the fitnesses by that value. When the likelihoods are

calculated though, the likelihoods are cumulative - this makes calculating the parents easy.

| Chromosome | Likelihood               |
|------------|--------------------------|
| 1          | (1/84)/0.135266 = 8.80%  |
| 2          | (1/24)/0.135266 = 30.8%  |
| 3          | (1/26)/0.135266 = 28.4%  |
| 4          | (1/133)/0.135266 = 5.56% |
| 5          | (1/28)/0.135266 = 26.4%  |

In program though, with the same initial values, the likelihoods would be cumulatively added - imagine it like the percentage of a pie chart. The first gene is from 0 to 8.80%, the next goes to 39.6% (because it *starts* from 8.8). The likelihood table would look like this:

| Chromosome | Likelihood (smi = 0.135266)      |
|------------|----------------------------------|
| 1          | (1/84)/smi = 8.80%               |
| 2          | (1/24)/smi = 39.6% (30.6+8.8)    |
| 3          | (1/26)/smi = 68% (28.4+39.6)     |
| 4 (0)      | (1/133)/smi = 73.56% (5.56+68)   |
| 5          | (1/28)/smi = 99.96% (26.4+73.56) |

The last value will always be 100 (in the above example, it isn't due to rounding). Now with the theory of it, let's look at the code. The code is very simple - note though that a type cast to float is required on the fitness value so that integer division doesn't occur. There are two functions, one to calculate the smi, and another to generate all the likelihoods.

```
float CDiophantine::MultInv() {
   float sum = 0;

   for(int i=0;i<MAXPOP;i++) {
      sum += 1/((float)population[i].fitness);
   }

   return sum;
}

void CDiophantine::GenerateLikelihoods() {
   float multinv = MultInv();</pre>
```

Ok, so now that we have the fitness and likelihoods values all set up, it's time to do some breeding!

#### **Breeding Functions**

The breeding functions are composed of three functions, one to get the gene index corresponding to a randomly generated number between 0 and 100, a function to actually calculate the crossover of two genes, and a main function to create the new population. We'll take the functions one at a time, seeing how they call each other. Here is the main breeding function:

So, we firstly create a temporary population of genes. Then we loop through all the genes. Now, when choosing genes we don't want the genes to be the same (no point mating with yourself:), and we don't need the genes to be the same either (that is where the operator== from the gene structure comes in handy). In choosing a parent, we generate a random number, then call the GetIndex function. GetIndex uses the idea of the cumulative likelihoods and merely iterates through the genes until it find the gene that contains that number:

```
int CDiophantine::GetIndex(float val) {
  float last = 0;
```

```
for(int i=0;i<MAXPOP;i++) {
    if (last <= val && val <= population[i].likelihood) return i;
    else last = population[i].likelihood;
}
return 4;
}</pre>
```

Returning to the CreateNewPopulation() function, you can also see that if the number of iterations exceeds MAXPOP squared, it will take any parents. After parents are chosen, we breed them, by passing the indices up to the Breed function. The Breed function returns a gene, which is put in the temporary population. Here's the code:

```
gene CDiophantine::Breed(int p1, int p2) {
  int crossover = rand() % 3+1;
  int first = rand() % 100;

  gene child = population[p1];

  int initial = 0, final = 3;
  if (first < 50) initial = crossover;
  else final = crossover+1;

  for(int i=initial;i<final;i++) {
     child.alleles[i] = population[p2].alleles[i];
     if (rand() % 101 < 5) child.alleles[i] = rand() % (result + 1);
  }

  return child;
}</pre>
```

Firstly we determine the crossover point. Now remember, we don't want the crossover to be the first or the last, because that entails copying over all or none of the second parent - pointless. We then create a random number that will determine when the first parents takes the initial crossover or not. The rest is self-explanatory - you can see that I've added a tiny mutation factor to the breeding. There's a 5% chance that a new number will occur.

#### And finally...

Now we can look at the Solve() function. It merely calls the above functions iteratively. Note that we test whether the function managed to find a result on the initial population - this is unlikely.

```
int CDiophantine::Solve() {
  int fitness = -1;
```

```
// Generate initial population.
 srand((unsigned) time(NULL));
 for(int i=0;i<MAXPOP;i++) {</pre>
    for (int j=0;j<4;j++) {
      population[i].alleles[j] = rand() % (result + 1);
    }
  }
 if (fitness = CreateFitnesses()) {
    return fitness;
  }
  int iterations = 0;
 while (fitness != 0 || iterations < 50) {
    GenerateLikelihoods();
    CreateNewPopulation();
    if (fitness = CreateFitnesses()) {
      return fitness;
    }
    iterations++;
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                              Electronic Theses & Dissertations
  return -1;
                              www.lib.mrt.ac.lk
}
```



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