දුන්ත**ාල** ටොරවුව විශ්ව වීද_{ා ලක} නු ලංකාව වෞරවට 91

EFFECT OF SOLIDS ON A PINCHED SLUICE CONCENTRATOR



A Thesis presented

to the

Department of Mining and Minerals Engineering

University of Moratuwa

Moratuwa, Sri Lanka

for the

DEGREE OF MASTER OF ENGINEERING

by

B. JEYADEVA

45309

October 1986

46309



To my wife,

for her understanding love and support

ABSTRACT

The pinched sluice concentrator is a device for the separation of heavy minerals particularly beach sands. They come in a variety of sizes and shapes and have been extensively used in the beach sand industry, for over a century. But the basic mechanism involved in the separation has not been fully understood.

Most of the work upto 1982, had been empirical in nature. In 1983, an attempt was made to explain the behaviour of pinched sluice in terms of established theories of fluid mechanics and mineral processing.

However, their work was limited to particles of single size. In the present analysis, an attempt has been made to refine the existing model, taking the effects of particle size and density into account.

The relationship between the flow rate and depth of flow was confirmed and their variation with particle size and feed concentration has been studied.

A method has been developed to calculate the underflow flow rate of the sluice assuming logarithmic velocity distribution and the established relationship between Froude Number and the split height.

Assuming that Bagnolds Shearing Theory holds in pinched sluice operations, and also the dispersive pressure is some function of solid concentration, velocity gradient, specific gravity and diameter of the particles, a relationship was derived to predict the underflow pulp density. Above relationship was used to predict the grade of the underflow for a mixture of ilmenite and silica.

ACKNOWLEDGEMENT

My sincere thanks and most grateful gratitude to my supervisor Dr. G.K.N.S. Subasinghe for his invaluable guidance and advice throughout this project. His constructive criticism and valuable suggestions during the preparation of the thesis is ackowledged with my grateful thanks.

I also wish to thank the Ceylon Institute of Scientific and Industrial Research (CISIR) for their financial assistance and its Director Dr. E.R. Jansz for his sincere help and cooperation.

The academic and technical staff of the Department of Mining and Mineral Engineering, University of Moratuwa for their help and cooperation.

I also thank Mrs. Padmini Perera, Mrs. Shirani Samaranayake and Mrs. Iranganie Bandara for an excellent job of typing and Anura and Mrs. Kanthi Gunasekera for the preparation of the figures and graphs.



CONTENTS

	Page
ABSTRACT	í
ACKNOWLEDGEMENT	ii
LIST OF FIGURES	viii
LIST OF TABLES	х
LIST OF SYMBOLS	хi
1. INTRODUCTION	
	1
2. BACKGROUND MATERIAL	4
2.1 Fluid	4
2.1.1 Properties of fluid	4
2.1.2 Properties of solid	9
2.1.3 Fluid flow condition	i 4
2.1.4 Bagnolds theory	17
2.2 Previous work on Pinched Sluices	20
2.2.1 Empirical approaches	20
2.2.2 Theoretical considerations	22
2.2.2.1 Development of flow rate, depth of flow relationship	22
2.2.2.2 Calculation of split height	24
2.2.2.3 Evaluation of underflow pulp density	27
2.2.2.4 Evaluation of grade of the underflow	28
3. EXPERIMENTATION	31
3.1 Equipment	31
3.1.1 The pinched sluice	31
3.1.2 Splitter arrangement	31

	Page
3.1.3 Slurry tank	31
3.1.4 Stirrer	31
3.1.5 Pump	34
3.1.6 Delivery pipe and valve	34
3.1.7 Distributor box	35
3.1.8 Depth measuring device	35
3.1.9 Sample collectors	37
3.1.10 The rig	39
3.1.ll Equipment used for the analysis of concentration and tailing sample	39
3.2 Materials	39
3.2.1 Size and size distribution	39
3.2.2 Density	41
3.3 Experimental Programme	42
3.3.1 Scope	42
3.3.2 Procedure	42
3.4 Discussion of experimental results	45
4. ANALYSIS AND DISCUSSION OF RESULTS	46
4.1 Underflow flow rate	47
4.1.1 Depth of flow, flow rate relationship	48
4.1.1.1 Derivation of the model	52
4.1.1.2 Effect of concentration	52
4.1.1.3 Effect of diameter	54
4.1.1.4 Discussion	59
4.1.2 Velocity distribution	60

		Page
4.1.3	Split height	60
4.1.4	Proposed model for the prediction of underflow flow rate	66
4.1.5	Comparison of the results	66
4.1.6	Discussion	69
4.1.7	Specimen calculation	69
4.2 Un	derflow pulp density	73
4.2.1	Velocity gradient	75
4.2.2	Solid concentration	76
4.2.3	Derivation of the model for the prediction of underflow concentration	77
4.2.4	Discussion	87
4.3 Gr	ade of underflow	91
4.3.1	Discussion	95
5. AP	PLICATION	99
5.1 Re.	fined Model	99
5.1.₹	Depth of flow	99
5.1.2	Split height	100
5.1.3	Underflow flow rate	100
5.1.4	Underflow pulp density	101
5.1.5	Underflow grade	101
5.2 Wo	cked Example	102
5.2.1	Calculation of depth of flow	102
5.2.2	Calculation of split height	103
5.2.3	Calculation of underflow flow rate	103
5.2.4	Calculation of underflow pulp density	104
5.2.5	Calculation of underflow grade	104
	(v)	

		Page
6.	CONCLUSION	105
6.3	l Depth of flow	105
	2 Split height	105
	Underflow flow rate	106
6.4		106
6.5		106
7.	FUTURE WORK	108
8.	APPENDIX 1 - Regression analysis - Theory	110
9.	APPENDIX 2 - Log-log plots of $Q_f/(B \sin \alpha^{\frac{1}{2}})$, for slurries of ilmenite, garnet and quartz of different diameter	112
10.	APPENDIX 3 - Log-log plots of $Q_f/(B \sin \alpha^2)$ for slurries of ilmenite, garnet and quartz of different diameter for different feed concentration ranges.	121
11.	APPENDIX 4 - Evaluation of intergral for Q _u (Section 4.1.3)	128
12.	APPENDIX 5 - Log-log of y' versus Fr for slurries of ilmenite, garnet and quartz of different diameter	129
3.	APPENDIX 6 - Plots of C _f /C _u versus y _o /U* for slurries of ilmenite, garnet, quartz of different diameter for different concnetration ranges	134
+ 0	APPENDIX 7 - Plot of C_u/C_f (observed) versus C_u/C_f (calculated) for ilmenite, garnet, quartz of different diameter	141

			Page
15.	APPENDIX 8 -	Observations	148
	A.8.1	Original Observations	148
	A.8.2	Reduced data	169
16.	LIST OF REFE	ERENCES	189

LIST OF FIGURES

- 2.1 Shock waves on converging walls
 - (a) at equal angles
 - (b) at different angles
- 3.1 Pinched sluice
 - (a) Plan and elevation
 - (b) Photograph of the sluice
- 3.2 Splitter arrangement
- 3.3 Distribution box
 - (a) Plan
 - (b) Photograph of the distribution box
- 3.4 Depth measuring device (photograph)
- 3.5 Sample collector (photograph)
- 3.6 The rig (photograph)
- 3.7 Magentic separator (photograph)
- 4.1 Longitudinal section through the centre line of the sluice
- 4.2 Log-log plot of $Q_f/(B \sin \alpha^{\frac{1}{2}})$ versus y_0 (line of best fit) for clear water, slurry of quartz, of different diameter, ilmenite and garnets.
- 4.3 Plot of gradient versus intercept of the log-log plot of $Q_f/(B \sin \alpha^{\frac{1}{2}})$ versus y_0 .
- Plot of gradient (log-log plot of $Q_f/(B \sin \alpha^{\frac{1}{2}})$ versus y_0) versus concentration
- Plot of gradient γ (log-log plot of $Q_f/(B \sin \alpha^{\frac{1}{2}})$ versus y_0) versus diameter
- .6(a) Plot of k, versus feed concentration
 - (b) Plot of M, versus feed concentration

- 4.7 Plot of y' (split height) versus Fr (Froude number) for clear water
- 4.8 Log-log plot of y' versus Fr, for clear water
- 4.9(a) Plot of underflow flow rate, observed versus calculated for clear water using the method proposed by substituting without the correction factor
 - (b) Plot of $Q_u(ob) \times \sin \alpha/Q_u$ (cal) versus Fronde number for clear water
- 4.10 Plot of underflow flow rate (observed) versus calculated for clear water using the proposed method
- 4.11 Plot of C_u/C_f versus U^*/y_0 for slurry of quartz (450 µm)
- 4.12 Plot of C_f/C_u versus y_0/U^* for slurry for quartz(450 µm)
- 4.13 Plot of gradient versus intercept (plot of C_f/C_u versus y_o/U^*) for ilmenite, garnet and quartz of different diameter
- 4.14 Plot of gradient versus intercept (plot of C_f/C_u versus y_0/U^*) for quartz of different diameter
- 4.15 Plot of gradient versus intercept (plot of C_f/C_u versus y_0/U^*) for ilmenite and garnet
- 4.16 Plot of gradient (plot of C_f/C_u versus y_o/U^*) versus feed concentration
- .17 Plot of $(M_2 0.013 C_f)$ versus diameter for quartz, ilmenite and garnet
- .18 Plot of C_u/C_f (observed) versus C_u/C_f (calculated)
 - (a) using Subasinghe's method
 - (b) using proposed method

- 4.19 Plot of concentration (by yol) of quartz observed versus calculated in the underflow, for a feed slurry consisting of ilmenite, quartz and water using the proposed methods.
- 4.20 Plot of concentration (by vol) of ilmenite observed versus calculated in the underflow for a feed slurry consisting of ilmenite, quartz and water using the proposed method
- 4.21 Plot of correction factor (ϕ) , versus specific gravity
- 4.22 Plot of G_u (calculated) versus G_u (observed) for feed slurry consisting of ilmenite and quartz and water

LIST OF TABLES

- Results of least square fit of the plot of the gradient(γ) (log log plot of $Q_f/(B \sin \alpha^{\frac{1}{2}})$ versus y_0) versus feed concentration.
- 4.2 Result of least square fit of the plot of gradient (γ) (log log plot of $Q_f/(B \sin \alpha^{\frac{1}{2}})$ versus y_0) versus diameter
- 4.3 Results of least square fit of log y' versus log Fr.

LIST OF SYMBOLS

В	Breadth of sluice
С	Volumetric concentration of solids
Co	C at closest packing
C _u	C of underflow
° _f	C of feed
c_1	Linear concentration of solids
c _d	Drag co-efficient
d	Particle diameter = Median apperture particle size (d ₅₀)
Fr	Froude number of flow
Frs	Fr at a section above the slot
g	Gravitational acceleration
Gu	Grade of under flow (volume fraction of heavies in the solids)
Gf	Grade of feed
K	Karman constant
L	Length of sluice
P	Bagnold dispersive pressure
Q	Total volumetric flow rate
$Q_{\mathbf{f}}$	Q of the feed
Q	Q of the underflow
R	solid recovery
Re	Renolds number of flow
Re p	Particle Renolds number
S	Specific gravity of solids
So	Slope of the sluice $\sin \alpha$
Ι, α	Slope of the sluice
t	Time
V	velocity of flow at an elevation

1126 Shear Velocity Ÿ Mean velocity of flow Vg Velocity of stream line satisfying gravity fall requirement The average velocity of underflow stream ·W Width of discharge slot У Elevation above the deck У Depth of flow y' Split height y" Height above boundary at which velocity is zero according to logrithmic distribution α Inclination of the sluice to the horizontal Exponent in equation 4.1 β Angle of shockwave with the direction of flow δ Nominal boundary layer thickness 81 Thickness of laminar sub-layer Eddy viscosity η Viscosity of pure fluid Kinematic viscosity of the fluid Density of fluid ρf Density of solids ρ Density of suspension Psus Angle of pinch of the sluice θ Shear stress at an elevation y Shear stress at the boundary τ_{o} Total shear stress due to the presence of grains and intergranular τΣ fluid Shear stress due to the presence of grains Shear stress due to the intergranular fluid. τ_{f}