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# RATIONALIZATION OF PRESTRESSED CONCRETE SPINE BEAM DESIGN PHILOSOPHY FOR EXPERT SYSTEMS

by  
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A thesis submitted to the University of Cambridge  
for the Degree of Doctor of Philosophy.



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Thesis

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January 1992

# Abstract

The most important aim of expert systems is to emulate the expert. The majority of existing expert systems for design try to achieve this by integrating the phases of the design process within one software environment thus achieving an overall automation. These integrated systems tend to support design by numerous repeated analysis due to their inability to suggest good preliminary solutions. The feedback from numerical analyses is needed to modify the preliminary solutions.

It is argued here that human experts have a different approach to design problems. They try to minimise the iterative nature of design by suggesting preliminary solutions which have a higher chance of succeeding at the subsequent detailed design stage. Expert systems should be able to do the same. Ideally, good preliminary solutions should be tailored to the requirements; this means that they should take account of the majority of constraints and structural behaviours quantitatively while selecting the values for key design parameters. It is suggested here that the numerical processing power of the computer should be used to obtain good preliminary solutions by developing design algorithms, which can take account of governing factors at an early stage of the design process. These in turn can be used to encapsulate knowledge in the expert systems instead of the 'heuristics' which are used to incorporate past experience in existing expert systems.

In order to develop these design algorithms, it is necessary to unravel the rationale behind each decision made during the preliminary design stage. In this thesis, the work carried out to rationalize the philosophy of the design process of prestressed concrete spine beams is explained in detail. The main advantage of this approach is that the expert system is compact and fast in execution. It is also capable of guiding the designer in a consultation session either by suggesting appropriate values or allowable ranges for key design parameters, as is done by a human expert.

**Keywords:** Prestressed Concrete, Spine Beams, Bridges (structures), Expert Systems, Prolog, Deep Knowledge



## Acknowledgements

I am most grateful to my supervisor, Dr C. J. Burgoyne, for introducing me to a topic related to expert systems and his interest, perseverance, guidance and friendship.

I have received much technical help from the computer officers of the Engineering Department, and in particular, wish to thank Mr Brian Wootton.

I also wish to thank to my friends in the Structures Group who made my time in Cambridge a memorable one. My gratitude to Ian Brown, Tim Ibell, Cam Middleton and Dr. Alan Kwan for proof reading my thesis.

Last, but not least, I wish to thank my wife, Chintha, for her unfailing support and encouragement.

Financial support from the Cambridge Commonwealth Trust, Lundgren Research Fund and Committee of Vice-Chancellors and Principles (in the form of an ORS award) is gratefully acknowledged, as is the support from SERC who made a grant available (Reference Number GR/F/31601) for purchase of computer hardware and software.

## Declaration

This thesis is a report of research work carried out in the Department of Engineering, University of Cambridge, between October 1988 and January 1991. Except where references are made to other work, the content of this thesis is original and includes nothing which is the outcome of work done in collaboration. The work has not been submitted in part or in whole to any other university. This dissertation is 250 pages.

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# Notation

$A_b$	Area of the bottom flange
$A_{b-min}$	Minimum area of the bottom flange allowed to prevent cracking
$A_{b-span}$	Required area of bottom flange at span critical section
$A_{b-support}$	Required area of bottom flange at support critical section
$A_c$	Area of the concrete section
$A_t$	Area of the top flange
$A_w$	Area of the web
$b_z$	Breadth of the section at a height $z$ from the bottom
$c$	Ratio between concrete cover required and depth of the section
$c_1$	Position of top fibre (measured from centroid, always -ve)
$c_2$	Position of bottom fibre (measured from centroid, always +ve)
$COR$	Cantilever Overhang Ratio as defined on page 105
$d$	Depth of the section
$e$	Eccentricity of prestressing cable (measured +ve downwards from centroid)
$e_{k1}, e_{k2}$	Eccentricity at kern points ( $Z_2/A_c$ ) and ( $Z_1/A_c$ )
$e_{min}$	Minimum eccentricity allowed considering cover limits
$e_{max}$	Maximum eccentricity allowed considering cover limits
$e_p$	Eccentricity of line of thrust
$e_{p-min}$	Minimum eccentricity of the line of thrust (upper bound)
$e_{p-max}$	Maximum eccentricity of the line of thrust (lower bound)
$e_s$	Eccentricity of actual cable profile
$e_1$	Distance to centroid of idealised top flange from the centroid of section
$e_2$	Distance to centroid of idealised bottom flange from the centroid of section
$E$	Young's modulus of the section
$E_z$	Young's modulus at a height $z$ from the bottom fibre
$f_c$	Permissible stress of concrete in compression
$f_{ct}$	Permissible stress of concrete in compression at transfer
$f_{cu}$	Characteristic cube strength of concrete
$f_{cw}$	Permissible stress of concrete in compression at working load
$f_t$	Permissible stress of concrete in tension
$f_{temp}$	Temperature stresses due to direct strain and curvature
$f_{tt}$	Permissible stress of concrete in tension at transfer
$f_{tw}$	Permissible stress of concrete in tension at working load
$I$	Second moment of area about centroid



$l_{l(i)}$	Distance measured to left change point from $i^{th}$ support
$l_{r(i)}$	Distance measured to right change point from $i^{th}$ support
$M$	External moments acting on the section
$M_a$	Minimum working load moment
$M_b$	Maximum working load moment
$M_f$	Moment range in one span (mid-span sagging less pier hogging)
$M_n$	Moment due to notional loads
$M_u$	Ultimate state moment acting on the cross section
$M_{2-min}$	Minimum reactant moment due to prestressing effects
$M_{2-max}$	Maximum reactant moment due to prestressing effects
$(M_2)_j$	Reactant moment at internal support j
$(M_t)_j$	Continuity moment at internal support j due to temperature
$n$	Number of supports
$N$	Number of webs of a box girder
$P$	Horizontal component of the prestressing force in cable
$P_B$	Cable force corresponding to point B of Magnel diagram
$P_{n(i)}$	Cable force in the new cable at the $i^{th}$ cable force change point
$P_{r(i)}$	Cable force in the running cable at $i^{th}$ cable force change point
$P_{su(i)}$	Cable force over $i^{th}$ support
$P_t$	Force in prestressing cable at transfer
$P_1$	Minimum prestress to satisfy moment range
$P_2$	Minimum prestress to satisfy lever arm
$P_3$	Minimum prestress for existence of line of thrust
$P_4$	Minimum prestress for existence of a line of thrust and maximum cable range
$R$	(Cable force at service)/(Cable force at transfer),
$RMR$	Reactant moment ratio as defined on page 64
$t_b$	Thickness of bottom flange
$t_l$	Linear transformation at left pier
$t_m$	Linear transformation at mid-span
$t_r$	Linear transformation at right pier
$t_t$	Thickness of top flange
$t_w$	Thickness of web
$t_z$	Temperature at a height $z$ above the bottom of the section
$w_b$	Width of the bottom flange
$w_s$	Clear spacing between webs
$w_t$	Width of the top flange

$x$	Distance measured to cross section from the left support
$z$	Distance measured from the bottom fibre
$\bar{z}$	Distance to centroid from the bottom fibre
$Z_1$	Section modulus for upper fibre, $I/c_1$ (always -ve)
$Z_2$	Section modulus for lower fibre $I/c_2$ (always +ve)
$\alpha$	Load factor for the ultimate limit state
$\alpha_c$	Coefficient of expansion of concrete
$\alpha_i$	( $i = 1, 2$ and $3$ ) Factors used to represent the idealised section as defined on page 84
$\alpha_{n(i)}$	Inclination of the anchor for new cable
$\alpha_{r(i)}$	Inclination of the running cable at force change point $i$
$\alpha_z$	Coefficient of thermal expansion at height $z$
$\beta$	(Lever arm at ultimate)/(depth of the section)
$\beta_j$	Distribution coefficient for $M_2$
$\beta_{ll(i)}$	Inclination of lower bound of cable profile at left hand side of the $i^{th}$ cable force change point
$\beta_{ur(i)}$	Inclination of upper bound of cable profile at right hand side of the $i^{th}$ cable force change point
$\delta$	(Maximum allowable concrete stress)/(Characteristic strength)
$\delta_i$	( $i = 1, 2$ and $3$ ) Factors used to represent the idealised section as defined on page 84
$\phi$	Diameter of the prestressing duct
$\phi_e, \phi_l$	Diameter of stirrups and longitudinal reinforcement in webs
$\psi$	Curvature due to temperature
$\epsilon_0$	Direct strain due to temperature
$\kappa$	Total curvature caused by prestressing effects

In addition to these symbols, a number of others symbols are defined and used locally.